The Dynamic Effects of Renewable Subsidies in the Green Energy Transition *

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November 6, 2023

Abstract

The speed at which electricity generation can transition to green energy sources depends in part on the incentives of coal and natural gas plants to enter or exit. I examine how government subsidies and the costs of renewables shape those strategies. To do so, I formulate a nonstationary dynamic model of generator entry and exit that incorporates heterogeneity in entry costs and nests it within a dynamic, hourly model of competition in the wholesale electricity market. I estimate the model using data from Texas. I find that renewable subsidies in place during the sample period reduce cumulative CO₂ emissions by 1.71 billion tons (or $62–$316 billion in environmental savings) through 2060, largely because they shift expectations about future competition and thereby reduce the entry of new coal plants in the early stage of the transition.

Keywords: carbon emissions, dynamics, electricity, entry and exit, renewable subsidies, start-up cost, nonstationarity

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*I am grateful to my advisors, Nathan Miller and John Rust, as well as Chenyu Yang and Şafak Yücel for their invaluable guidance and support. I thank Caué Dobbin, Sharat Ganapati, Raphael Calel, Luming Chen and seminar participants at Georgetown University for helpful comments.

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1 Introduction

The green energy transition requires a radical change in the energy sources used to generate electricity. Government subsidies have long been used to encourage earlier and faster expansion of clean energy, such as that derived from wind and solar energy. For example, the US provided $75 billion in tax subsidies over 2005-2020 to support renewables (Kirshenberg 2018; EIA 2023b), and this is projected to reach $220 billion by 2030 under the Inflation Reduction Act (Bistline et al., 2023). The effectiveness of these subsidies depends not only on their direct impact on renewables, but also on how they affect expectations of future profitability for coal and natural gas generators.

In this paper, I examine the effects of renewable subsidies on the green energy transition and carbon emissions along the transition path. To understand how these subsidies have affected the observed transition path, and how they will affect future outcomes, I develop an annual nonstationary equilibrium model of generator entry and exit that accounts for long-run trends in electricity demand, natural gas prices and renewable installation costs. The model nests a secondary dynamic model of the wholesale electricity market where all generators compete to produce electricity each day during peak and off-peak hours, and coal and natural gas generators are subject to start-up costs. The nested hourly model determines annual profits in the annual model. I estimate the model using data from Texas over 2005–20. Among estimation results are that the entry costs of coal generators are significantly larger than those of natural gas generators, and that renewables cannibalize more profits from coal than natural gas because of the differences in their fuel costs and operation and maintenance costs.

I use the model to evaluate the effects of renewable subsidies. I focus on the effects of a long-standing set of renewable subsidies, including production tax credits (PTCs) and investment tax credits (ITCs) that large phased out over 2016-2020. I find that those subsidies significantly reduce coal entry in the initial years, despite negligible renewable capacities during that period. Therefore the dynamic model indicates that subsidies can have an impact even before the renewables start to expand. Simulation shows that those subsidies decrease carbon emissions by 1.7 billion tons through 2060, and 66% of the reduction comes from the reduced coal expansions. Subsidies with longer horizons can further divert demand from dirty coal to less dirty natural gas, leading to an additional environmental benefits, but it can increase generation costs over some periods. Overall, my analysis provides insight into how long-lasting renewable subsidies can reduce carbon emissions and highlights the mechanisms by which the duration of subsidies influences the policy effects.

The paper proceeds as follows. In Section 2, I provide an overview of renewable subsidies in the US and institutional details of electricity market in Texas, and also describe my data sources. The annual data include capacities of different energy sources before 2020, along with statistics about multiple profit shifters, including demand, input prices and engineering estimates of renewable installation costs. The hourly data include detailed information about electricity demand, electricity prices, generation from wind and solar, fuel costs and outputs from all coal and natural gas generators in 2020. I use the annual data to document the long-term trends in market forces, and use the hourly data to demonstrate the main characteristics of electricity demand and generation from different energy sources. Both long-run trends and those characteristics are important for generator profits; therefore, they inform the following empirical analysis.

I introduce the nonstationary dynamic model in Section 3. I assume that coal and natural gas generators make entry and exit decisions, and that wind and solar generators make entry decisions, all
conditional on current and (expected) future demand, costs, and subsidies. Thus, a feature of the model is that generators anticipate and respond to not only future policy changes but also reactions to those future changes from other generators (i.e., equilibrium feedback effects as in [Holland et al.](#) (2022)). The model is nonstationary because it incorporates time-varying renewable entry costs (varying due to changes in subsidies and renewable installation costs across years) and profit shifters, which together shape the incentives of generators to enter and exit. One challenge when solving the model is that a curse of dimensionality exists with many generators, as there are in Texas. To reduce the state space for the entry and exit model, I adopt the nonstationary oblivious equilibrium (Benkard et al., 2008) in which generators can make near-optimal decisions by tracking only calendar time $t$ instead of capacities of different types of generators.

Payoffs in the annual model are provided by an hourly model of competition in the wholesale electricity market. The hourly model is also used to evaluate carbon emissions and generation costs under different compositions of coal, natural gas, and renewables along the transition path. I present the hourly model in Section 4. I model two aggregate shocks: residual demand (electricity demand net of renewable generation) and natural gas prices. The volatility of these shocks affects how coal and natural gas generators operate, determining electricity prices and generator profits. When nested in the annual model, the distribution of these shocks changes because of long-run trends and differences in renewable capacities, and it therefore shifts generator profits.

Turning to the operation of large coal and natural gas generators in the hourly model, I assume that they make two decisions. They first choose whether to operate (start-up decision) subject to start-up costs, a fixed cost incurred when a generator switches from off to on. Then, operating generators choose their output to maximize profits within a constrained range. The literature has identified the substantial impacts of start-up costs on generator profits and how profits would be affected by renewable expansions (Mansur, 2008; Cullen, 2011; Cullen, 2013; Reguant, 2014; Jha and Leslie, 2021; Gowrisankaran et al., 2022). Similarly to previous literature, I model the start-up decisions as dynamic discrete choices. However, aggregate shocks, which are typically simplified in the previous literature, and the large number of generators create another curse of dimensionality, posing difficulties in both solving and estimating the model. Inspired by Gowrisankaran et al. (2022), I reduce the state space by adopting the moment-based equilibrium (Iffrach and Weintraub, 2017) for the hourly model, assuming that generators make start-up decisions based on aggregate shocks and only the previous total output from coal and gas generators. The hourly model allows for rich interactions among different energy sources under various demand and input-price conditions. This capability is necessary when the model is nested within the annual model for the entire transition process.

Next, I discuss estimation methods and present estimation results in Section 5. I estimate the hourly model using two steps. First, I estimate the hour-specific distributions of electricity demand, wind and solar utilization factors, and natural gas prices. The estimated distributions replicate the main characteristics of the electricity market, including the hourly cyclical patterns in electricity demand, the intermittency of renewable generation, and the large volatility of natural gas prices. Second, I estimate variable operation and maintenance costs of generating electricity and start-up costs associated with large coal and natural gas generators via the simulated method of moments. The estimates deliver a good model fit: the simulation matches well electricity generation and operating frequencies of each type of generators, as well as electricity prices at different hours. Simulations based on the estimated model give reasonable estimates of annual generator profits. The simulated carbon emissions for the period
between 2005–2020 match closely with the actual data, showcasing its strong ability to extrapolate to different years.

With annual profits from the hourly model, I then calibrate parameters related to generator entry and exit for the annual model, ensuring that coal and natural gas capacity trends align between data and model simulations. The calibration reveals that coal’s entry cost per MW is nearly three times greater than that of natural gas. The positive correlation between entry costs and carbon emissions rates drives the entry and exit decisions of coal and natural gas generators and their environmental consequences.

Using the model, I evaluate the impacts of renewable subsidies between 2005 and 2020 in Section 6. I simulate the transition path until 2060 with and without subsidies, and compare the carbon emissions between the two paths. The subsidies reduce carbon emissions by 1.71 billion tons through 2060; however, instead of fastening phase-out of incumbent coal and natural gas generators, 66% of carbon savings come from a reduction of coal expansions by 3.8GW in the initial years, despite a mere 0.85GW increase in wind during that time. This pattern cannot be explained by a static model. Instead, the subsidies encouraging more renewables increase future competition and therefore deter the entry of coal. Besides generating environmental benefits, renewable subsidies also significantly reduce generation costs by $46.5 billion, largely because of reduced natural gas expansions in the middle of the energy transition. Considering the $14.6 billion increase in investment, this reduction in generation costs shows that, despite the politically contentious social cost of carbon, the economic benefits from subsidies make a strong case for adopting them.

Finally, I study how the time horizon of subsidies affects the energy transition and the environmental and economic surpluses along the transition path. Under alternative horizons, three effects in the transition dynamics are important. First, the entry of renewables tends to cluster in years when the subsidies are about to expire. Second, either early bunching or later but more aggressive expansion of renewables can prevent coal entry in the early stage of the energy transition. Third, the capacity of natural gas peaks in the middle of energy transition, especially between 2020 and 2030. I compare carbon reductions and social returns for subsidies with different lengths. I find that among subsidies that generate similarly large carbon reductions, 16-year subsidy gives the highest social returns.

Section 7 concludes the paper and provides directions for future research. As a major climate policy tool, renewable subsidies have been implemented for multiple decades, with considerable tax expenditures on them. In this paper, using Texas as an example, I evaluate the effects of renewable subsidies in place between 2005 and 2020 over the entire transition path through 2060. I carefully consider the contemporary long-run trends in market forces and the equilibrium feedback effects. The majority of the effects on carbon reduction come because the subsidies shape the expectation about future competition and shift the entry decisions of coal generators. My analysis also shows that the length of subsidies needs to be carefully designed, taking into account the bunching of renewables and the different equilibrium responses from coal and natural gas generators. Beyond Texas, the empirical framework can be generalized to study the effects of subsidies in broader regions or to examine the impacts of other nonstationary policies.

1.1 Related Literature

I contribute to a literature that examines the dynamic effects of climate policies in the electricity market (Linn and McCormack 2019; Gowrisankaran et al. 2023; Eisenberg 2020; Abito 2020; Gowrisankaran et al. 2022; Gonzales et al. 2023; Johnston et al. 2022; Elliott 2022; Holland et al. 2022; Stock and
Stuart, 2021; Gillingham et al., 2021; Palmer et al., 2011; Borenstein and Kellogg, 2023), and more broadly in heavy-polluting industries (for example, Ryan, 2012 and Fowlie et al., 2016). The two papers that are closest to mine are Gowrisankaran et al., (2022) and Elliott (2022), both of which examine the impacts of environmental policies on generator entry and exit in a nonstationary environment. Gowrisankaran et al., (2022) study how uncertainty surrounding the Mercury and Air Toxics Standard (MATS), a policy mainly targeting polluting coal power plants, affects their technology adoption and exit of them. The time horizon of subsidies has similar effects to policy uncertainty, as it shifts the power plants’ expectations. In my paper, instead of focusing on only one energy source, I study the equilibrium responses to the subsidies from not only wind and solar but coal and natural gas, which are the main sources of carbon emissions. Elliott (2022) studies the impacts of environmental regulation on the electricity market, focusing on the balance between reducing carbon emissions and enhancing reliability. Elliott does not consider coal and natural gas generators’ dynamic decisions, which depend on start-up costs, partly because generators in the market he studies are relatively small. In this paper, these dynamics are explicitly modeled in the nested hourly model so that the model better reflects how much large generators in Texas respond to renewable expansions.

The hourly model builds on an extensive literature studying competition in the wholesale electricity market and the role of start-up costs (Borenstein et al., 2002; Bushnell et al., 2008; Wolak, 2007; Reguant, 2014; Gowrisankaran et al., 2016; Mansur, 2008; Fowlie, 2010; Cullen, 2011; Reguant, 2014; Jha and Leslie, 2021). I extend the literature by incorporating aggregate shocks including demand and input prices, and incorporating the effects of energy storage, following Karaduman (2020), so that the hourly model is rich enough to reflect how profits change along the entire transition path. My paper also relates to the literature that employs either the competition models or reduced-form methods to examine the short-run impacts of renewable expansions on carbon emissions and market operations (Kaffine et al., 2013; Novan, 2015; Bushnell and Novan, 2021; Fell and Kaffine, 2018; Jha and Leslie, 2021; Gowrisankaran et al., 2016; Karaduman, 2021; Cullen, 2011). This paper contributes to the literature by modelling dynamics to demonstrate that the sustained presence of subsidies can cause those impacts even before renewable expansion starts. Also, this paper examines those impacts not only in a short period but along the entire transition path.

Finally, in both the annual model and the hourly model, I build on the recent literature approximating Market perfect equilibrium using oblivious strategies (Weintraub et al., 2008; Weintraub et al., 2010; Benkard et al., 2008; Ifrach and Weintraub, 2017) to overcome the curse of dimensionality due to a large number of generators. I apply the nonstationary oblivious equilibrium (Benkard, 2004) to the annual model and employ the moment-based equilibrium (Ifrach and Weintraub, 2017) in the hourly model. This provides a tractable framework for examining issues in a large market where both long-run decisions and short-run decisions have dynamic considerations.

Both nonstationary oblivious equilibrium and moment-based equilibrium are widely used equilibrium concepts in the literature. Recent applications of nonstationary oblivious equilibrium include Caouil (2023) and Johnston et al. (2022). Recent applications of moment-based equilibrium include Jeon (2022), Vreugdenhil (2020), Gerarden (2023), and Gowrisankaran et al. (2022). Gowrisankaran et al. (2022) extend it to approximate belief oligopoly equilibrium by allowing firms to recognize the impacts of their actions on a reduced set of market states.
2 Institutional Details and Data

2.1 Renewable Subsidies in the US

In this section, I describe renewable subsidies between 2005 and 2020, and the extension of renewable subsidies in the Inflation Reduction Act of 2022. To quickly reduce carbon emissions, significant renewable subsidies were established to encourage earlier adoption of renewable energy sources, including wind and solar. The main subsidies considered in this paper are PTCs and ITCs. The ITC is primarily qualified by solar projects and is calculated as a percentage of a project’s investment cost. Before 2020, the ITC was 30%, but it was reduced in 2020 and 2021. The PTC, typically applicable to wind projects, is given annually and available for 10 years, in an amount equal to a specified credit rate multiplied by the amount of electricity generated. The credit rates (2020 dollars) before 2022 are plotted in Figure 2a. They remained constant before 2017 and were gradually reduced until 2021. I convert PTC into a lump-sum payment, similar to the ITC. To achieve the goal of zero emissions, the Inflation Reduction Act of 2022 extended renewable subsidies for at least 10 years at a rate of $24.8 for the PTC and at 30% of installation costs for the ITC. They will be phased out either in 2032 or when carbon emissions in the power sector reach 25% of their 2022 levels, whichever comes later.

2.2 ERCOT Market

The Electric Reliability Council of Texas (ERCOT) is an independent system operator that manages the majority of the electricity grid in Texas. It schedules electricity flow on a grid that connects 46,500 miles of transmission lines and serves more than 26 million customers. In 2020, 45.5% of electricity generation in ERCOT came from natural gas, 22.8% from wind, 17.9% from coal, 10.9% from nuclear, and 2.9% from other sources including solar, hydro and petroleum coke. Residential consumption accounts for 51.3% of electricity demand in ERCOT, while the commercial sector represents 30.9%, and the industrial sector the remaining 17.8%.

Multiple institutional features of ERCOT inform the empirical analysis. First, ERCOT separates itself from Eastern and Western interconnections as shown in Figure A-1. This isolation makes it unnecessary to include imports and exports in the analysis.

Second, the majority of generators in ERCOT are deregulated. Regulated generators are subject to cost-of-return regulation and operate in accordance with rates established by regulatory authorities, rather than being responsive to wholesale prices. Deregulated generators and regulated generators also differ in their incentives regarding when to retire their capacity.

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2 Beyond tax credits, renewable portfolio standards (RPS) provide an additional incentive for adopting renewable capacity. RPS requires that a specified percentage of the electricity suppliers sell comes from renewable resources. Texas first adopted an RPS in 1999; it required the state to install 5 GW of new renewable energy capacity by 2015 and set a target of 10 GW of renewable energy capacity by 2025. However, the RPS was not binding because Texas had already reached its 2025 goal in 2009; therefore, I do not consider RPS in this paper.

3 For example, assume that PTC is $24/MWh and the utilization factor of a wind project is 40%. Then the PTC for 1GW of wind capacity is $84.10 million per year. The equivalent lump-sum payment, assuming that the PTC will last for 10 years, is therefore $841 million.

4 86% of coal and natural gas generators in my sample are owned by investor-owned utilities.

5 Gowrisankaran et al. (2023) show that the speed of coal generators’ retirement is slower in regulated states because utilities in regulated markets are authorized to charge sufficient rates to recover investment under “used
Third, there is no capacity market in ERCOT. A capacity market provides a subsidy for installed capacity, and the subsidy does not depend on energy production. It is designed to guarantee a sufficient reserve capacity to meet peak demand and prevent blackouts (Fabra 2018). In the absence of capacity market payments, the sole incentive for market entry is the profits generated from producing and selling electricity.

Fourth, market concentration in ERCOT is very low. In 2020, there were 58 utilities and HHI at the utility level was 360. Consequently, the exercise of market power is limited during most hours throughout the year, as evidenced by the significantly lower prices in comparison to other regions. Large utilities often strategically hold off some generators to reduce output and increase prices. Since there is no evidence of high market power, I do not consider the ownership linkage across generators.

2.3 Data

The data contain an annual component for the entry and exit model, and an hourly component for the wholesale competition model. The dataset is compiled from various sources, all public available.

The primary dataset used for the hourly model is the Continuous Emissions Monitoring System (CEMS) database from the Environmental Protection Agency. It includes hourly electricity generation (MWh), heat input (MMBtu) and carbon emissions (tons) for almost all thermal generators in the US. I screen out generators in Texas but not covered by ERCOT according to their county. Based on CEMS data, I construct several important characteristics of generators. I define the capacity of a generator as the 95th percentile of its hourly output between 2005 and 2020; and similarly to Gowrisankaran et al. (2022), I define a generator’s minimum output requirement as the modal generation level in hours when output is in between the generator’s 5th and 25th percentiles throughout the sample. The heat rate (MMBtu/MWh) is constructed as the ratio of annually total heat input to total output, and the CO₂ emission rate (tons/MWh) is the average mass of carbon divided by hourly output. The remaining characteristics, including primary energy source and technology, come from EIA form 860.

Next, I combine the primary dataset with data about fuel costs. For deregulated power plants, plant-level input prices are not available in EIA. So I apply average input prices in Texas to all generators. I collect daily natural gas prices ($/MMBtu) from Henry Hub, and annual average coal prices in Texas from EIA.

I then merge in wholesale electricity prices, electricity demand, and wind and solar generation, all at hourly level. I collect day-ahead wholesale electricity prices for each hour in multiple zones from Energy Online and take the average across zones. Electricity load, wind output, and solar output are from the ERCOT website. The hourly utilization factors of wind and solar are calculated as the ratio of output to annual capacity.

Finally, the annual capacities of coal, natural gas, wind, and solar between 2010 and 2020 are aggregated from EIA-860. The wind and solar capacity-expansion forecasts are from Department of Energy and Asmelash and Prakash (2019) respectively. The installation costs of wind and solar between and useful principal, which requires generators to be physically used and useful to ratepayers even if it is not efficient to use them.

Footnotes:

8The Capacity and minimum output requirement for generators are also provided in EIA form 860; however, it is not a one to one mapping between a unit in CEMS and a generator in EIA (Huetteman et al. 2021). Since the main analysis is at unit level using CEMS data, I do not use capacity and minimum output requirement information in EIA 860.

2013 and 2020 are reported by EIA, and the forecasts in 2030 and 2050 are provided by Irena (2019) and Olson and Bakken (2019) respectively.

2.4 Data Description

Energy Transition in ERCOT Figure 1 shows annual capacities of the main energy sources for electricity generation in ERCOT. The most remarkable change in the fuel mix is the expansion of renewables. Wind capacity started to increase in 2005 and has accelerated since 2014. Solar capacity began to grow in 2018 and increased by 10 GW within four years. Regarding fossil fuel generators, ERCOT exhibited a steady increase of natural gas capacity. There was an increase in coal capacity between 2005 and 2015. The Clean Power Plan essentially forbid the establishment of new coal generators after 2015 and coal generators start to retire. Nuclear and hydro power account for a small share of electricity generation in ERCOT, and they remain stable over time. Therefore, I assume that the capacity of nuclear and hydro power will remain the same in the future.

![Figure 1: Capacity by Primary Energy Source](image)

Notes: I calculate capacity by primary energy source using data from EIA 860. Generators that temporarily disappear in EIA 860 are assumed to continue operating in gap years.

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8 I consider on-shore wind only. In 2020, only 2% of wind capacity came from off-shore wind farms, and their share is projected by US Department of Energy to increase to only 4% in 2050 (Department of Energy, 2023).

9 There are mainly three technologies for natural gas generators in ERCOT: combined-cycle gas turbine, open-cycle gas turbine, and steam turbine. I focus on combined-cycle gas turbines because they account for the majority of natural gas generators in ERCOT.
Contemporary Trends  Besides renewable subsidies, multiple other trends contribute to the changes in ERCOT’s fuel mix. First, the installation costs of wind and solar fell sharply between 2005 and 2020, and they are projected to fall even further. The main driving forces of the cost reduction are R&D and learning by doing (Rubin et al., 2015; Bollinger and Gillingham, 2019; Covert and Sweeney, 2022). Since demand for wind turbines and solar photovoltaic from ERCOT accounts for a tiny share of global production, I assume the decline in installation costs is exogenous. Another technology advancement comes from the shale gas revolution. The combination of hydraulic fracturing and horizontal drilling significantly increased the production of natural gas and reduced the natural gas price from $9.4/MMBtu to $2.0/MMBtu between 2005 and 2020, as shown in Figure 2d.10 The price of coal is stable over time because most power plants and coal mines are vertically integrated and prices are determined by long-term contracts. Finally, electricity demand has been increasing since 2005 because of continued population growth in Texas, and demand in peak hours and off-peak hours has increased in parallel.

10The natural gas price jumped to $7.5/MMBtu in 2022 temporarily because of production freeze-offs in the first quarter and high net withdrawals from storage, but it returned to $4/MMBtu in October (EIA, 2023a).
Notes: Panel (a) shows historical rates of PTCs for wind projects and ITCs for solar projects between 2005 and 2020. Absent the Inflation Reduction Act, I assume that both PTCs and ITCs would have gradually phased out. IRA 2022 extended both subsidies by at least 10 years (Bistline et al., 2023). In the empirical analysis, the PTC is converted into a lump-sum payment as an ITC, on the assumption that the utilization factors of wind will remain the same in the next 10 years.

Panel (b) shows engineering estimates of installation costs for on-shore wind and solar panels. Data between 2010 and 2020 come from EIA, and they are assumed to be constant before 2010. Installation costs for utility-scale solar are projected to decrease by 50% by 2050 compared with 2020 (Olson and Bakken, 2019). For wind, I follow Irena (2019), who estimates that installation costs of on-shore wind will be $0.8–$1.35 million/MW in 2030 and $0.6–$1 million/MW in 2050. I use the midpoints of these intervals and linearly interpolate the installation costs between 2020 and 2030 and between 2030 and 2050.

Panel (c) plots the annual averages of electricity demand in peak hours and off-peak hours. Before 2022, they are calculated from hourly load data in each year. I project future demand according to the business-as-usual case in Choukulkar (2022) except that I assume that demand remains constant after 2040.

Panel (d) plots annual averages of natural gas prices and coal prices. Natural gas prices before 2022 are calculated from daily Henry Hub natural prices, and coal prices in Texas come from EIA. I assume that natural gas prices will remain at $4.08/MMBtu after 2022.
Hourly Wholesale Electricity Market  Electricity is distinct from other commodities because of multiple unique characteristics of its demand and supply. These attributes play a crucial role in shaping generators’ profits of generators under alternative fuel mixes, and they therefore determine the incentives for entry and exit in the long run.

First, electricity demand is inelastic with respect to electricity prices. Second, demand varies cyclically over the course of a day as illustrated in Figure 3a, which displays the mean and 5th–95th percentiles of electricity demand by hour in 2020. Electricity demand typically peaks between 1 p.m. and 8 p.m. and plummets at night and in the early morning. Peak hours also exhibit larger variation across days than do off-peak hours. Third, given capacity, wind and solar generation are exogenous, contingent upon the intensity of wind and sunlight. Figure 3c plots the mean and 5th–95th percentiles of utilization factors for wind and solar. Comparing that figure with Figure 3a illustrates the intermittency of renewable generation. Wind generation cannot rise when demand peaks and solar generation is limited to daytime. Additionally, the variability in wind and solar generation across days amplifies the fluctuations in residual demand (demand net of renewable generation) faced by coal and natural gas generators.

Each hour, coal and natural gas generators make two types of decisions. First, they decide whether to operate, taking into account the start-up cost, a fixed cost incurred when a generator switches from being idle to producing any positive amount. It includes substantial fuel costs and opportunity costs arising from potential boiler-equipment damages. Figure 3b plots the probability of operating by hour of day for coal and natural gas separately. More than 80% of coal generators and about 60% of natural gas generators choose to be on at night, when electricity prices are even lower than fuel costs. This suggests that both coal and natural gas generators are subject to significant startup costs. However, compared with peak hours, at night 20% less natural gas and almost no coal is idle. This suggests that natural gas generators have much smaller start-up costs than coal generators. Second, conditional on operating, coal and natural gas generators decide how much to produce with an increasing marginal cost curve and subject to a limited range of output levels. The maximum output of a generator is constrained by capacity, which is determined at the time of construction and remains fixed over time. The minimum output requirement sets a lower bound for output; Producing below it results in inefficiency and equipment damages. Figure 3d plots the utilization factors of coal and natural gas generators when they are on. As prices rise from $15/MWh at 5 a.m. to $55/MWh at 5 p.m., the utilization factor of coal increases from 50% to 80%, about two times the response from natural gas generators. This suggests a steeper marginal cost curve for coal than natural gas.

11 Absent smart metering and real-time pricing, very few consumers are willing and able to adjust their consumption to price fluctuations in the wholesale market.
Figure 3: Operation Characteristics of Hourly Electricity Market

Notes: All panels use data from ERCOT in 2020.
- Panel (a) shows the mean and 5th–95th percentiles of electricity demand by hour of day.
- Panel (b) shows mean electricity prices by hour of day and the operation probabilities for coal and natural gas generators.
- Panel (c) shows the mean and 5th–95th percentiles of capacity factors by hour of day for wind (upper panel) and solar (lower panel).
- Panel (d) shows mean electricity prices by hour of day and utilization factors conditional on operation for coal and natural gas generators.

I categorize generators into two groups: dominant and fringe. I model the operation of individual dominant generators in greater detail, including their dynamic start-up decisions and output decisions. As for the fringe generators, I group all of them as a representative subject. It makes a single static output decision, subject to an increasing marginal cost curve, without start-up costs or output constraints. The distinction between dominant and fringe generators is based on their sizes and operation frequencies. Smaller generators, which have significantly lower start-up costs, and generators that operate only during a very short period in a year, are not considered for dynamic decisions. Specifically, a generator is considered dominant if it meets two criteria: (1) capacity exceeds 100 MW and (2) it operated for...
more than 60% of all hours in at least one year between 2005 and 2020. In 2020, dominant generators constituted 80% of all coal and natural gas generators.

Table 1 provides summary statistics of the dominant generators. I consider three types of generators: coal, small natural gas, and large natural gas. I assume there is no heterogeneity within each type and use the mean as the representative attribute for each type. Coal generators have considerably larger capacity than natural gas generators. Minimum output accounts for a substantial portion of the capacity: 42% for coal generators, 66% for small gas generators and 54% for large gas generators. Natural gas generators are typically more fuel efficient than coal generators, as measured by heat rates. Carbon emission rates from natural gas generators are about half of coal generators’ rates, which implies that replacing coal with natural gas will benefit the environment. However, since natural gas generators still produce substantial carbon emissions compared with renewables, it is desirable to gradually phase them out in the end.

### Table 1: Summary Statistics of Dominant Generators

<table>
<thead>
<tr>
<th></th>
<th>Coal</th>
<th>Natural Gas: Small</th>
<th>Natural Gas: Large</th>
</tr>
</thead>
<tbody>
<tr>
<td>Capacity (MW)</td>
<td>741.63</td>
<td>252.06</td>
<td>421.29</td>
</tr>
<tr>
<td></td>
<td>(163.05)</td>
<td>(51.08)</td>
<td>(100.82)</td>
</tr>
<tr>
<td>Minimum Output Requirement (MW)</td>
<td>313.00</td>
<td>167.26</td>
<td>228.50</td>
</tr>
<tr>
<td></td>
<td>(123.26)</td>
<td>(40.08)</td>
<td>(14.57)</td>
</tr>
<tr>
<td>Heat Rate (MMBtu/MWh)</td>
<td>9.89</td>
<td>7.58</td>
<td>6.98</td>
</tr>
<tr>
<td></td>
<td>(0.69)</td>
<td>(1.38)</td>
<td>(0.45)</td>
</tr>
<tr>
<td>CO₂ Emission Rate (tons/MWh)</td>
<td>1.06</td>
<td>0.47</td>
<td>0.44</td>
</tr>
<tr>
<td></td>
<td>(0.06)</td>
<td>(0.08)</td>
<td>(0.04)</td>
</tr>
<tr>
<td>N</td>
<td>19</td>
<td>78</td>
<td>14</td>
</tr>
</tbody>
</table>

**Notes:** The table provides summary statistics of coal and natural gas generators whose capacity is larger than 100MW and who operate in more than 60% of the hours in at least one year between 2005 and 2020. Natural gas generators are further categorized as small or large based on whether their capacity is less than 300MW. Characteristics of generators are calculated based on Continuous Emissions Monitoring System data (see Section 2.3).

### 3 Annual Entry and Exit Model

In this section, I present the annual nonstationary dynamic model of generator entry and exit. I employ the model to simulate the transition paths — that is, capacities of different energy sources under different policy scenarios.

Time is discrete with infinite horizon \( t = 0, 1, 2, \ldots \). I assume that there exists a terminal period \( T \) after which all coal and natural gas generators are forced to exit and there is no further entry of wind and solar. In other words, the market remains a steady state after \( T \).

There are five types of generators \( j \in J = \{\text{coal}, \text{small natural gas}, \text{large natural gas}, \text{wind}, \text{and solar}\} \), and generators within each type are homogeneous and indexed by \( i \). Generators make independent entry and exit decisions. Period profit of a generator with type \( j \) is determined by a deterministic function \( \pi(K_t, z_t) \), where \( K_t = (K_t^{\text{coal}}, K_t^{\text{small gas}}, K_t^{\text{large gas}}, K_t^{\text{wind}}, K_t^{\text{solar}}) \) represents the incumbent capacity of each energy source and \( z_t = (z_t^{d}, z_t^{g}, z_t^{b}) \) are profit shifters associated with electricity demand, natural gas prices, and the effects of energy storage. The profit function is microfounded in the hourly competi-
tion model, which is introduced in the next section. \( \{K_t\}_{t=0}^{\infty} \) is endogenously determined by generator entry and exit, and I assume that generators have perfect foresight about \( \{z_t\}_{t=0}^{\infty} \).

The timeline before period \( T \) is as follows:

- Incumbents and potential entrants observe market state \((K_t, t)\). Incumbent coal or natural gas generators also privately observe independent scrap value \( \phi^j_{it} \sim F^{\phi,j} \).
- Each generator forms expectations over the evolution of future \( K_t \).
- Based on current period profits, future profit shifters, and expectations about future capacity of different energy sources, incumbent coal and natural gas generators decide whether to exit. Incumbent wind and solar generators never exit the market.
- Potential entrants of all types decide whether to enter the market. If they enter, coal and natural gas generators pay fixed entry costs \( \psi^j \), \( j \in \{\text{coal, small natural gas, large natural gas}\} \), and the entry costs associated with wind and solar are time varying and calculated as installation costs \( I^j_t \) net of subsidies \( \Gamma^j_t \), \( \psi^j_t = I^j_t - \Gamma^j_t \), \( j \in \{\text{wind, solar}\} \).
- Finally, each generator acts on its entry/exit decision and \( K_t \) evolves accordingly.

Calendar time \( t \) plays an important role in the model. First, profit shifters exhibit long-run trends. Second, the installation costs are declining over time. Third, the renewable subsidies are time dependent. Generators keep track of \((K_t, t)\) in the Markov perfect equilibrium (MPE). It is a sixth-dimension object and therefore imposes a curse of dimensionality. To reduce the state space in this nonstationary environmental, instead of MPE, I adopt non-stationary oblivious equilibrium as proposed by Benkard et al. (2008). It exploits the fact that when there are many generators, for each type, the effects on total capacity from individual-generator entry and exit almost wash out. Therefore, when coupled with the assumption that generators are infinitesimal \(^{12}\) capacity of different energy source follows roughly a deterministic trajectory. Specifically, suppose that generators of type \( j \) use common strategy \( \zeta^j_t (K_t, z_t) \), which represents the probability of exit in period \( t \), and there are new entrants of mass \( \lambda^j_t \), \( j \in \{\text{wind, solar}\} \). Then the expected capacity of each energy source follows

\[
\begin{align*}
\tilde{K}_{t, \text{coal}} &= \tilde{K}_{t-1, \text{coal}} (1 - \zeta^\text{coal}_t) + \lambda^\text{coal}_t \\
\tilde{K}_{t, \text{gas:small}} &= \tilde{K}_{t-1, \text{gas:small}} (1 - \zeta^\text{gas:small}_t) + \lambda^\text{gas:small}_t \\
\tilde{K}_{t, \text{gas:large}} &= \tilde{K}_{t-1, \text{gas:large}} (1 - \zeta^\text{gas:large}_t) + \lambda^\text{gas:large}_t \\
\tilde{K}_{t, \text{wind}} &= \tilde{K}_{t-1, \text{wind}} + \lambda^\text{wind}_t \\
\tilde{K}_{t, \text{solar}} &= \tilde{K}_{t-1, \text{solar}} + \lambda^\text{solar}_t,
\end{align*}
\]

with \( \tilde{K}_0 = K_0 \). Therefore instead of tracking \((K_t, t)\) and forming expectations about \( K_t \), generators can approximate future profits using \( \tilde{K}_t \) and therefore make near-optimal decisions by tracking only calendar time \( t \).

The following Bellman equation characterizes the dynamic programming problem of an incumbent coal or natural gas generator:

\(^{12}\)I assume generators are infinitesimal to avoid the integer problem in the state transition process, similarly to Cullen and Reynolds (2023).
\[ V_t^j(\phi_{it}^j) = \Pi_t^j(\tilde{K}_t, z_t) + \max\{\phi_{it}^j, \beta E[V_{t+1}^j(\phi_{it+1}^j)]\}. \] (2)

The ex ante value function (before the realization of \( \phi_{it}^j \)), \( V_t^j \), is given by

\[ V_t^j = \Pi_t^j(\tilde{K}_t, z_t) + \eta_t^j E[\phi_t^j | \phi_t^j \geq \beta V_{t+1}^j] + (1 - \eta_t^j)\beta EV_{t+1}^j, \]

where \( \zeta_t^j = E[I{\phi_t^j \geq \beta V_{t+1}^j}] \) represents the probability of exit in period \( t \), with \( I{\cdot} \) being an indicator function. I further assume that scrap values follow independent exponential distributions with mean \( \bar{\phi}^j \).

Then,

\[ \zeta_t^j = \exp\left\{ -\frac{\beta V_{t+1}^j}{\bar{\phi}^j} \right\} \]

and

\[ E[\phi_t^j | \phi_t^j \geq \beta V_{t+1}^j] = \bar{\phi}^j + \beta V_{t+1}^j. \]

I assume that there is a large pool of potential entrants for each energy source. If each potential entrant plays a symmetric mixed entry strategy, following Weintraub et al. (2008), the capacity of new entrants is approximated by the Poisson distribution with a state-dependent mean, \( \lambda_t^j \), which is determined by free-entry conditions. Specifically,

\[ \psi_t^j \leq \beta V_{t+1}^j \text{ implies } \lambda_t^j = \overline{\lambda} \]
\[ \psi_t^j = \beta V_{t+1}^j \text{ implies } \lambda_t^j \in (0, \overline{\lambda}) \]
\[ \psi_t^j \geq \beta V_{t+1}^j \text{ implies } \lambda_t^j = 0. \] \hspace{1cm} (3)

where \( \overline{\lambda} \), the cap of capacity from new entrants in each year, is assumed to be the same across energy sources. \(^{13}\)

The nonstationary oblivious equilibrium is defined as follows. It contains a set of strategies \( \{\eta_t^j, \lambda_t^j\}_{t=0}^T \) for \( j \in J \) such that in each period \( t \),

(a) \( \eta_t^j \) solves the Bellman equation (2), and

(b) \( \lambda_t^j \) satisfies free-entry conditions (3).

To solve for the equilibrium, I start from a set of initial guesses of \( \{\eta_t^j, \lambda_t^j\}_{t=0}^T \) for \( j \in J \) and calculate the expected transition path following (1) and profits \( IV(\tilde{K}_t, z_t), j \in J \). Next, I solve the Bellman equations (2) by backward induction and check the free-entry conditions (3). I then update the exit strategies \( \{\eta_t^j\}_{t=0}^T \) based on strategies from two consecutive iterations and update the entry strategies \( \{\lambda_t^j\}_{t=0}^T \) depending on the extent of the violation of the free-entry conditions. An equilibrium is solved if exit strategies \( \{\eta_t^j\} \) from two consecutive iterations are close enough and free-entry conditions are satisfied by \( \{\lambda_t^j\} \) for all \( j \in J \). The details of the algorithm are provided in Appendix II.

\(^{13}\)The inclusion of the cap for capacity from new entrants is motivated by the constraint posed by the interconnection queue. To build a new power plant and connect it to transmission lines, new entrants first need to go through an interconnection queue in which the system operator conducts studies to evaluate their impacts on the grid. Only a few studies can be conducted, which sets a limit on the amount of newly built capacity in each year. Even though it can take on average four years for a generator to get through the interconnection queue in the US in general, the process is much faster in ERCOT (Clifford, 2023). Therefore, I assume that time to build is only one year.


4 Hourly Model of the Wholesale Electricity Market

In this section, I describe the hourly model of competition in the day-ahead wholesale electricity market. Each hourly model corresponds to one period in the entry and exit model. It is associated with a specific value for the profit shifters, \( z_t \), and a fixed set of incumbent generators with capacity \( K_t \). The usefulness of the model is twofold. First, the annual profits are calculated by simulating the model and aggregating hourly profits for a year. Annual profits under model simulations with alternative \((K_t, z_t)\) serve as payoffs in the entry and exit model. Second, carbon emissions and generation costs are evaluated by solving for the hourly model along the transition paths out of the entry and exit model.

The model is designed to capture the main characteristics of the electricity market as presented in Section 2.4. I collapse 24 hours in a day into two model hours: one peak hour and one off-peak hour. Electricity demand and renewable generation are random variables with different distributions at peak hours and off-peak hours. In each hour, dominant coal and natural gas generators first decide whether to operate taking into account start-up costs \(^{14}\) and then choose output to maximize profits with an increasing marginal cost and subject to a limited ranges of output \(^{15}\).

I model the start-up decision as a dynamic discrete choice problem in spirit of Rust (1987), similarly to Cullen (2011) and Gowrisankaran et al. (2022) \(^{16}\). I deviate from them in two ways. First, demand and renewable generation enter the market as aggregate shocks. They shape the residual demand faced by coal and natural gas generators, impacting both their operation and profits. Incorporating the aggregate shocks enables me to analyze how shifts in demand and the growth of renewable capacity affect generator profits when integrating the hourly model into the annual model. Secondly, rather than assuming a constant marginal cost and limiting the output to be either at full capacity or at the minimum requirement, I consider an increasing marginal cost and allow for any generation level ranging from the minimum output requirement to the full capacity, similarly to Reguant (2014). My specification allows the marginal cost to increase at different rates for coal and natural gas generators, as suggested in Section 2.4. This difference has implications for how generators’ profits would change with price reductions from renewable expansions \(^{17}\).

One challenge when solving for the model is the curse of dimensionality from the large number of generators in the market. When deriving the optimal strategy of choosing whether to operate, generators form expectations about future prices by tracking aggregate shocks, including residual demand and natural gas prices, and the number of generators of each type operated in the previous hour. This creates

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\(^{14}\) Collapsing 24 hours into 2 model hours implicitly assumes that generators commit to keeping the same operation status within each windows. This is consistent with data showing that it is rare for a generator to switch its status more than once within a day. It also should be nonproblematic for the counterfactuals because variations in demand and renewable generation occur mainly across days and between peak hours and off-peak hours. The variability within the peak-hour and off-peak-hour time windows is limited.

\(^{15}\) I do not consider ramping costs — that is, adjustment costs when generators change their output levels rapidly, conditional on operation. Reguant (2014) finds that ramping costs are not significant for coal or CCGT generators under a specification with an increasing marginal cost.

\(^{16}\) Other studies modelling start-up costs include Reguant (2014) and Jha and Leslie (2021). Reguant (2014) models the role of start-up costs in the context of multi-unit auctions, Jha and Leslie (2021) model start-up costs as mainly fuel costs, which may be appropriate for natural gas generators but is probably inappropriate for large coal generators, where the opportunity costs from equipment damages can be significant.

\(^{17}\) Both the slope and intercept of marginal cost affect how generators’ profits change in response to a price adjustment. Consider a firm with a quadratic marginal cost \( C(q) = aq + bq^2 \) in a competitive market with the price \( p \). The impact of a price change on the generator’s profit is given by \( \frac{\partial \pi}{\partial p} = \frac{p - a}{2b} \). The effect is influenced by both parameters, \( a \) and \( b \).
a large state space with a complicated transition rule. I reduce the state space by solving for a moment-based equilibrium (Ifrach and Weintraub [2017]). Instead of tracking operation status of all generators, I assume that generators make their start-up decisions based on total output from dominant coal and natural gas generators in the previous hour, $Q_{h-1}$, which as a moment, summarizes the information about how many generators operated in the previous hour.

Next, I lay out the details of different components of the hourly model.

**Electricity Demand**  There are infinite number of hours within one period, $h = 1, 2, 3, \cdots$ with two types $l_h \in \{O, P\}$ alternating, where $O$ stands for off-peak hours and $P$ represents peak hours.

Electricity demand $d_h$ is assumed to be inelastic with respect to electricity price and given by

$$d_h = z^d_t d^{l_h} + \varepsilon^d_h,$$

where $d^{l_h}$ is the mean electricity demand for hour type $l_h$ and $\varepsilon^d_h$ follows an AR(1) process with hour-type-specific coefficients:

$$\begin{align*}
\varepsilon^d_h &= \rho^d_l \varepsilon^d_{h-1} + \sigma^d_l \eta^d_h \\
\eta^d_h &\sim \mathcal{N}(0, 1) \\
\eta^d_h &\perp \varepsilon^d_{h'}, \quad h \geq h'.
\end{align*}$$

In each period the demand shifter $z^d_t$ is fixed, but across periods both means and standard deviations of electricity demand change in both peak and off-peak hours.

**Generation from Wind and Solar**  Wind and solar capacities, $K^W_t$ and $K^S_t$, remain fixed within a period. The utilization factor of wind in hour $h$, $\omega^W_h$, is a random variable with similar stochastic structure to electricity demand:

$$\begin{align*}
\omega^W_h &= \omega^{W,l_h} + \varepsilon^W_h \\
\varepsilon^W_h &= \rho^{W,l_h} \varepsilon^W_{h-1} + \sigma^{W,l_h} \eta^W_h \\
\eta^W_h &\sim \mathcal{N}(0, 1),
\end{align*}$$

where $\omega^{W,l_h}$ is the mean during hours of type $l_h$, and $\rho^{W,l_h}$ and $\sigma^{W,l_h}$ are hour-type-specific AR(1) coefficients. The utilization factor of solar in hour $h$, $\omega^S_h$, follows

$$\begin{align*}
\omega^S_h &= \omega^{S,l_h} + \sigma^{S,l_h} \varepsilon^S_h \\
\varepsilon^S_h &\sim \mathcal{N}(0, 1),
\end{align*}$$

where $\omega^{S,l_h}$ is the mean during hours of type $l_h$ and $\sigma^{S,l_h}$ is the hour-type-specific standard deviation of shocks to solar utilization factors. There is almost no persistence in $\varepsilon^S_h$ across hours for solar in the data, therefore, I assume away the AR(1) structure for solar.

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18Even though the purpose of the hourly model is to collect annual profits, I assume an infinite horizon to avoid non-stationarity. It is computationally difficult to compute models combining both non-stationarity and aggregate shocks.
Given realizations of $\omega^W_h$ and $\omega^S_h$, without curtailment, electricity generation from wind and solar is given by

\[ q^W_h = K^W_t \times \omega^W_h \]
\[ q^S_h = K^S_t \times \omega^S_h. \]

In the absence of energy storage, electricity supply from renewables in hour $h$ comprises the generation from wind and solar in that hour ($q^W_h$ and $q^S_h$). With zero marginal costs for wind and solar, they meet the electricity demand first, leaving a residual demand for coal and natural gas generators as

\[ d^r_h(0) = d_h - (q^W_t + q^S_t), \]

where $d^r_h(0)$ represents the residual demand when energy storage level $z^b_t = 0$. The introduction of energy storage, as measured by a parameter $z^b_t$, smooths the fluctuations of residual demand, $d^r_h(z^b_t)$, across hours. When generation from renewables exceeds demand, I assume that residual demand becomes zero and wind and solar are curtailed proportionally to their output. The details of energy storage and curtailment are given in Appendix III.

**Fuel Prices** I assume that coal prices are fixed at $p^c$ and natural gas prices follow an AR(1) process:

\[ p^g_h = z^g_t \mu^g + \rho^g p^g_{h-1} + z^g_t \sigma^g \varepsilon^g_h, \quad \varepsilon^g_h \sim \mathcal{N}(0, 1). \]

The natural gas price shifter, $z^g_t$, changes both the mean and volatility of natural gas prices across periods.

**Electricity Generation by Fringe Generators** Small or infrequently operating generators are classified as fringe generators. I assume that these fringe generators are homogeneous and not constrained by either minimum output requirements or capacity limitations. Similarly to Butters et al. (2021), I assume that the marginal cost of fringe generators has an exponential form:

\[ mc^f = \exp\{c^f_0 + c^f_1 Q^f_h + \sigma^f \eta^f_h\}, \quad \eta^f_h \sim \mathcal{N}(0, 1), \]

where $Q^f_h$ is the output from fringe generators in hour $h$, and $\eta^f_h$ is an unobservable that captures any hour-specific market-level shocks that can affect electricity prices. $\eta^f_h$ is assumed to be independent from all other random variables. Given electricity price $p_h$, the output from fringe generators is given by

\[ Q^f_h = \frac{\log p_h - c^f_0 - \sigma^f \eta^f_h}{c^f_1}. \]

**Electricity Generation from Dominant Generators: Production Decisions** In each hour, dominant generators first decide whether to operate (the start-up decision) taking into account startup costs, and then they decide how much to produce (the production decision). Denote the set of dominant generators that operate in hour $h$ as $G^+_h$, which is determined by generators’ start-up decisions (specified
next). Generator $i$ of type $j$ in $G_i^+$ chooses output to maximize its profit\textsuperscript{19}:

$$\pi_{ih} = \max_{q_{ih}} p_h q_{ih} - C^j(q_{ih}; \eta_{ih})$$

$$q^j_i \leq q_{ih} \leq q^j_i,$$

where $q_{ih}$ is the output of generator $i$ in hour $h$. Generator $i$’s output is constrained by the minimum output requirement $q^j_i$ and capacity $q^j_i$. $C^j(q_{ih}; \eta_{ih})$ is the cost of producing $q_{ih}$ and I assume that it has the following functional form:

$$C^j(q_{ih}; \eta_{ih}) = (p^j_h \times H^j + \mu^j + \sigma^j \eta_{ih})q_{ih} + \frac{\alpha^j}{2q^j}(q_{ih} - q^j_i)^2$$

$$\eta_{ih} \sim \mathcal{N}(0,1),$$

where $(q_{ih} - q^j_i)_+ = \max\{q_{ih} - q^j_i, 0\}$. The cost consists two parts. First, fuel costs are the product of fuel price $p^j_h$ ($$/MMBtu$$) and heat rate $H^j$ (MMBtu/MWh), which measures the fuel efficiency of generators of type $j$. Second, all costs except fuel costs are variable operational and maintenance (O&M) costs. They are assumed to be quadratic; Therefore, generators have a linearly increasing marginal cost. $\mu^j$, associated with fuel cost and a cost shock $\eta_{ih}$, determines the intercept of marginal cost. $\alpha^j$, associated with capacity $q^j_i$, determines the slope of marginal cost. Appendix \textsuperscript{IV} derives the optimal output $q_{ih}$ given electricity price $p_h$ and expected profit $E[\pi_{ih}|p_h]$ when $\eta_{ih}$ is integrated out.

**Equilibrium Price** The equilibrium price in each hour is determined by balancing demand and electricity generation from all energy sources:

$$\sum_{i \in G_i^+} q_{ih}(p_h; \eta_{ih}) + Q_f^I(p_h) = d^I_r(b_t)$$

The operational characteristics of dominant generators and inelastic demand present challenges in establishing equilibrium prices. I will discuss these challenges in two cases:

**Case I: Excess Supply from Dominant Generators**

When the combined minimum output of all dominant generators committed to production surpasses the residual demand ($\sum_{i \in G_i^+} q_{ih} \geq d^I_r(b_t)$), the equilibrium price may not exist because the electricity demand is inelastic to the electricity price. In such a case, I assume that excess electricity supply is freely disposed of, causing the electricity price to drop to its lowest possible value\textsuperscript{20}. However, such scenarios are rare because $G_i^+$ is endogenously determined by generators’ equilibrium start-up strategies and generators aim to avoid situations where they would incur losses.

**Case II: Insufficient Supply from Dominant Generators**

Next, consider the case in which the residual demand is not fulfilled when all operating dominant generators produce at their minimum output requirements ($\sum_{i \in G_i^+} q_{ih} < d^I_r(b_t)$). In this case, challenges regarding the existence of equilibrium prices emerge due to the output constraints of dominant generators. Limited by their capacity, it may be insufficient for dominant generators to meet all electricity

\textsuperscript{19}Type $j$ is linked to generator $i$. I represent it as $j$ when there is no ambiguity.

\textsuperscript{20}I set the lowest value of the electricity price as the intercept of the fringe marginal cost. Setting the lower bound as zero generate almost the same results.
demand. To overcome this, I assume that the representative fringe generator has no capacity constraint. So the fringe can always fill the gap between demand and generation from dominant generators.

A more subtle challenge in establishing the equilibrium price comes from minimum output requirements, which result in multiple flat steps in the aggregate electricity supply curve. I address this issue by incorporating idiosyncratic shocks, $\eta_{ih}$, to the intercept of marginal cost, reducing the length of those plateaus. In any case where the demand realization falls within the middle of a flat step, residual demand is adjusted by curtailing renewable generation to achieve equilibrium.

An alternative method to tackle the challenges associated with establishing equilibrium prices is to consider the possibility of blackouts. However, I implicitly assume away blackouts because of the flexibility of fringe supply. Nonetheless, my model can provide insights into the reliability issues in the electricity market by analyzing electricity prices. In situations where there’s inadequate capacity from dominant generators, electricity prices can experience sharp increases.

**Electricity Generation from Dominant Generators: Start-Up Decisions** Before discussing the details of start-up decisions, I lay out the timing assumptions.

- At the beginning of each hour, electricity demand $d_{ih}$, renewable productivity $\omega^W_{ih}$, and natural gas price $p^G_{ih}$ are realized.
- Observing the total output from dominant generators in the previous hour ($Q_{h-1}$), the electricity demand ($d_{ih}$), the capacity factor of wind ($\omega^W_{ih}$), the capacity factor of solar ($\omega^S_{ih}$), and the natural gas price ($p^G_{ih}$), each dominant generators decide to operate, as captured by the indicator variable, $\chi_{ih}$, after observing an idiosyncratic shock associated with each action, $\xi_{ih}$.
- Marginal shocks associated with dominant generators, $\eta_{ih}$, and fringe generators, $\eta^f_{ih}$ are realized. Fringe generators and generators in $G^+$ choose their output and earn profits.
- Electricity is consumed, and the market moves to the next hour.

I focus on the moment-based equilibrium in which generators make start-up decisions using strategies based on states $\{\chi_{ih-1}, d_{ih}, p^G_{ih}, Q_{h-1}\}$. The following Bellman equation characterizes the dynamic programming problem when making start-up decisions:

$$V^*_i(\chi_{ih-1}, d_{ih}, p^G_{ih}, Q_{h-1}) = E_{\varepsilon_{ih}} \max \left\{ \sigma^j_{ih-1} + \beta W^j_{0}(d_{ih}, p^G_{ih}, Q_{h-1}), \sigma^j_{ih-1} + \Pi^j(d_{ih}, p^G_{ih}, Q_{h-1} - \kappa^j) \{ \chi_{ih-1} = 0 \} + \beta W^j_{1}(d_{ih}, p^G_{ih}, Q_{h-1}) \right\},$$

(4)

where $\chi_{ih}$ is an indicator function that takes the value of 1 when a generator operates. $\Pi^j(d_{ih}, p^G_{ih}, Q_{h-1})$ is type-$j$ generator’s perceived expected profits in hour $h$. $\kappa^j$ is the start-up cost incurred when a generator of type $j$ switches from off to on. $\varepsilon = \{\varepsilon^0_{ih}, \varepsilon^1_{ih}\}$ follow independent type I extreme value distributions with mean 0 and scale parameter $\sigma^j$. $W^j_{0}(d_{ih}, p^G_{ih}, Q_{h-1})$ and $W^j_{1}(d_{ih}, p^G_{ih}, Q_{h-1})$ are choice-specific value functions as in Rust (1987). They give continuation values associated with operation decisions in hour $h$. Given the distribution assumption for $\varepsilon$, $W_0$ and $W_1$ are given as follows:

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21 Each step is associated with at most one generator due to the idiosyncratic shock $\eta_{ih}$. Consequently, only a small margin of curtailment from wind generation is needed to reach an equilibrium. The minimum wind capacity in periods I study is 1.7GW, sufficient for the adjustment.
A moment-based equilibrium consists of a set of belief parameters \( \theta \) and a set of start-up strategies. The equilibrium is defined as a solution to a system of equations that represent the expected profit of all generators.

The equilibrium is given by

\[
W^{j,\lambda}_1(d^r_h, p^g_h, Q_{h-1}) = E^{d^r_{h+1}, p^g_{h+1}, Q_{h}} V^{s,h+1}_1(1, d^r_{h+1}, p^g_{h+1}, Q_{h})
\]

\[
= E^{d^r_{h+1}, p^g_{h+1}, Q_{h}} \sigma^j \log \left\{ \frac{\Pi^{j}(d^r_{h+1}, p^g_{h+1}, Q_{h}) + \beta W^{j,\lambda+1}_1(d^r_{h+1}, p^g_{h+1}, Q_{h})}{\sigma^j} \right\}
\]

\[
+ \exp \left\{ \frac{\beta W^{j,\lambda+1}_0(d^r_{h+1}, p^g_{h+1}, Q_{h})}{\sigma^j} \right\}
\]

where the expectation is taken over a perceived transition kernel that specifies the perceived distribution of \( d^r_{h+1}, p^g_{h+1}, Q_{h} \) given \( d^r_h, p^g_h, Q_{h-1} \) when the market moves from hour type \( l_h \) to \( l_{h+1} \).

Next, I discuss the perceived transition kernel and the perceived expected profits. One challenge when using the moment-based equilibrium is that the moment \( Q_{h-1} \), which summarizes the operation status of all generators, might not follow a Markov process because part of the information is lost when aggregating individual operation status to their total output. Following Gowrisankaran et al. (2022) and Barwick et al. (forthcoming), I approximate the transition process of \( Q_{h-1} \) by a parametric AR(1) process. Specifically, I assume that the perceived transition rule of \( Q_h \), conditional on \( d^r_h \) and \( p^g_h \), follows

\[
Q_h = \theta_{l_h}^d + \theta_{1}^{d_h} d^r_h + \theta_{2}^{p_h} p^g_h + \theta_{3}^{\eta_h} Q_{h-1}, l_h \in \{O, P\}.
\]

Though simple, the AR(1) specification is able to capture the effect of residual demand and natural gas prices on dominant generation and, therefore, the electricity price. \( Q_{h-1} \) captures the possible state dependence due to the start-up cost.

Given the perceived transition kernel, the perceived single-hour profit of type-\( j \) generators is then given by

\[
\Pi^{j}(Q^f_h) = E[E[\pi_{ih} | p_h(Q^f_h; \eta^f_h)] | Q^f_h],
\]

where the inner expectation is taken over the perceived transition kernel and the transition of \( d^r_h \) (since \( Q^f_h = d^r_h - Q_h \)), and the outer expectation is taken over \( \eta^f_h \).

**Definition of the Moment-Based Equilibrium** A moment-based equilibrium consists of a set of start-up strategies \( \chi_{ih}^{l_h}(\chi_{ih-1}, d^r_h, p^g_h, Q_{h-1}) \) for generator \( i \) of type \( j \) \( \in \{ \text{coal, small natural gas, large natural gas} \} \) and a set of belief parameters \( \theta^{l_h} = \{ \theta_{0}^{d_h}, \theta_{1}^{d_h}, \theta_{2}^{p_h}, \theta_{3}^{\eta_h} \} \) for \( l_h \in \{O, P\} \) such that

(a) \( \chi_{ih}^{l_h}(\chi_{ih-1}, d^r_h, p^g_h, Q_{h-1}) \) solves the Bellman equation \( (4) \)

(b) \( \theta^{l_h}, l_h \in \{O, P\} \) are consistent with simulated data generated from \( \chi_{ih}^{l_h}(\chi_{ih-1}, d^r_h, p^g_h, Q_{h-1}) \)

\[\text{22} \]I calculate the outer expectation using 8th-order Gauss-Hermite quadrature.
Algorithm I describe the algorithm used to compute the moment-based equilibrium. The details of the algorithm are provided in Appendix V. To compute the equilibrium, I start from a set of candidate belief parameters \( \theta^l_h, l_h \in \{O, P\} \). Then, I compute the transition matrix of \( (d^r_h, p^g_h, Q_h) \) by discretizing the AR(1) process associated with \( \theta^l_h, l_h \in \{O, P\} \). Next, I solve the start-up strategies \( \chi_{ih}^{l_h}(\chi_{ih-1}, d^r_h, p^g_h, Q_{h-1}) \) as solutions to the Bellman equation (4). I then forward simulate the start-up decisions and output decisions of all generators in the market and collect \( Q_h \) for a large-enough number of hours \( H \). Next, I update the belief parameters by estimating regressions of \( Q_h \) on \( d^r_h, p^g_h \) and \( Q_{h-1} \) by employing OLS, separately for peak hours and off-peak hours. An equilibrium is achieved if the belief parameters in two consecutive iterations are close enough.

Annual Outcomes Having solved for the moment-based equilibrium, I calculate the annual profits of different types of generators as well as total generation costs and carbon emissions. The calculation is a by-product of the forward simulation step in the algorithm solving for the equilibrium. For a dominant generator \( i \), the profit is given by

\[
\Pi^i_t = E\left[ \sum_{h=1}^{365 \times 2} (p^i_h q^i_h - C^{\Pi}(q^i_h; \eta^{i}_{ih})) H^i_h - \kappa^i I\{\chi_{ih} = 1, \chi_{ih-1} = 0\} + \varepsilon^{\chi_{ih}} \right],
\]

where the expectation is taken over different simulation draws of \( \{\eta^f_h, \eta^s_{ih}, \varepsilon^{\chi_{ih}}\} \), and \( H^i_h \), which maps one peak hour to 8 data hours and one off-peak hour to 16 data hours. The profits have four components, revenue, generation costs, start-up costs, and a revenue correction term for the type I extreme value shocks.

The profits of wind and solar are given as follows:

\[
\Pi^i_t = \sum_{h=1}^{365 \times 2} p^i_h q^W_h H^i_h - C^W,
\]

\[
\Pi^i_t = \sum_{h=1}^{365 \times 2} p^i_h q^S_h H^i_h - C^S,
\]

where \( q^W_h \) and \( q^S_h \) are output from wind and solar, and \( C^W \) and \( C^S \) are annual fixed O&M costs for wind and solar.

Total generation costs include fuel costs, variable O&M costs and start-up costs for dominant generators, annual fixed costs for wind and solar, as well as costs for fringe generation. The costs for the representative fringe generator is

\[
C^{fringe}_t = \sum_{h=1}^{365 \times 2} H^i_h \int_0^{Q^i_h} \exp\{c^f_0 + c^f_1 q + \sigma^f \eta^f_{ih}\} dq = \frac{\exp\{c^f_0 + \sigma^f \eta^f_{ih}\}}{c^f_1} (\exp\{c^f_1 Q^i_h\} - 1).
\]

I take the average of various outcomes across multiple 730-hour windows and generators of the same type in the forward simulation step of the solution algorithm for the moment-based equilibrium.
Annual carbon emissions out of electricity generation from type-$j$ generators are given as follow:

$$Q_{t,\text{carbon}} = \sum_{i \in G_n^j} \sum_{h=1}^{365 \times 2} \tau^j q_{ih} H_h$$

where $\tau^j$ is the emission rate of CO$_2$ (tons/MWh) from generators of type $j$. Electricity generation from fringe generators also produce carbon emissions. I assume that fringe generators have the same carbon emission rates as natural gas generators.

5 Estimation and Calibration

In Section 5.1 I discuss the identification and estimation of parameters in the hourly model. Then, I present the estimation results and model fits. In Section 5.2 to illustrate the effects of competition between different energy sources, I present the first-order approximation of the profit surface, which is trained by a deep neural network. Finally, in Section 5.3 I discuss how I calibrate parameters in the annual entry and exit model.

5.1 Estimation of Generation Costs and Start-up Costs

I apply the hourly model to ERCOT data in 2020. I first collapse the original data across 24 hours in a day into 2 model hours, as detailed in Appendix I. I then conduct the estimation in two steps. First, I estimate distributions of aggregate market variables including electricity demand, wind and solar utilization factors, and natural gas prices. In the second step, I jointly estimate generation costs and start-up costs associated with dominant generators and marginal costs associated with fringe generators via simulated method of moments. The parameters to be estimated in the second step are summarized in $\Xi$:

$$\Xi_{\text{hourly}} = \{ \alpha^j, \mu^j, \sigma^c,j, \kappa^j, \sigma^j, c_f^j, c_f^1, \sigma^f \}$$

The estimation procedure goes is nested. In the inner loop, I solve for the moment-based equilibrium, simulate the model for $T$ periods, and calculate moments from the simulated data. In the outer loop, I search for the parameters that best match simulated moments and data moments.

5.1.1 Identification

I discuss in this section the identification of cost parameters. Parameters in the O&M costs are identified from the first-order condition of dominant generators’ profit-maximization problem. As shown in Appendix IV without output constraints, the utilization factors $q_{ih}^*/\bar{q}^j$ are proportional to electricity prices $p_{ih}$ net of fuel costs $p_{ih}^f H^j$ when a generator is on. By focusing on observations when the output is strictly in between $\bar{q}^j$ and $\bar{q}^j$, the positive correlation between electricity prices and utilization factors identifies $\alpha^j$, and the average and standard deviation of utilization factors help identify $\mu^j$ and $\sigma^{c,j}$. 
The identification of start-up costs is similar to Cullen (2011). First, consider generators’ start-up decisions without start-up costs and the associated type I extreme value shocks. In this case, the start-up decisions follow a cutoff rule (Rust [1987]): regardless of previous operation status, generators will choose to operate if the expected profits are above zero; otherwise, they are off. However, with start-up costs present, generators remain operating when the expected profits are moderately negative to avoid future start-up costs. Therefore, \( \kappa^j \) are identified by the differences in probability of operating when generators have the same expected profits but different operation status in the previous hour. Given that fuel costs account for a substantial share of start-up costs, I parameterize \( \kappa^j, j \in \{ \text{small natural gas, large natural gas} \} \) as

\[
\kappa^j = \kappa^j_0 + \kappa^j_1 p^g_h.
\]

\( \kappa^j_1 \) is identified by the difference in the probability of operating under various natural gas prices. The scale parameters \( \sigma^j \) can be identified by comparing the operational probabilities in the model incorporating those unobserved shocks with the probabilities in a deterministic model. Finally, the marginal cost curve of the representative fringe generator is identified by the correlation between the fringe output and the electricity price.

The moments used in the estimation are (1) the mean and standard deviation of utilization factors across different residual demand realizations when generators operate without their output constraints being binding; (2) the probability of a generator turning on after being off, across five residual demand realizations; (3) the same probability as in (2), but for generators operated in the previous hour; (4) the probability of a generator turning on after being off, across different natural gas prices; (5) the probability of a generator operating, separately for each type of hours; (6) electricity prices and total output from different types of generator, separately for each type of hour.

5.1.2 Estimation Results

Electricity Demand, Renewable Productivity, and Natural Gas Prices  Table A-1 summarizes electricity demand, and wind and solar utilization factors by hour. Despite being collapsed into two hours, they are consistent with the descriptions in Section 2.4. Tables A-2 and A-3 report estimates of hour-specific AR(1) processes for shocks to electricity demand and wind utilization factors. The correlation coefficient between \( \eta^d_h \) and \( \eta^w_h \) is 0.0485, supporting the assumption that demand shocks \( \eta^d_h \) and shocks to wind production \( \eta^w_h \) are independent.

Natural gas prices exhibit remarkable persistence, characterized by an AR(1) coefficient of 0.99. The accompanying constant of 0.02 indicates an average natural gas prices of approximately $2/MMBtu in 2020. The standard deviation of AR(1) residuals is 0.056, corresponding to a volatility of natural gas prices that is at approximately $0.4/MMBtu. This underscores the substantial fluctuations in natural gas prices.

Estimate of Cost Parameters  Table 2 reports estimates of cost parameters. The estimates are consistent with the main characteristics in the operation of coal and natural gas generators as discussed in Section 2.4. The slope of marginal costs, which are determined by \( \alpha^j \) and capacity, is $0.014/MWh^2 for natural gas generators, approximately twice as high as for coal ($0.0064/MWh^2). The values of \( \alpha^j \) and \( \mu^j \) jointly determine O&M costs. At maximum capacity, O&M costs for small natural gas and coal
generators are $5.63/MWh and $6.10/MWh, close to the engineering estimates of variable O&M costs in [Mann et al. (2017)], $4.73/MWh and $6.33/MWh for natural gas and coal generators respectively.

The estimated start-up cost associated with coal generators is $0.69 million per start-up, similar to [Gowrisankaran et al. (2022)] estimate of $0.6 million for the start-up cost for 600MW coal generators. Start-up costs are $0.03 million for small generators and $0.09 million for large generators. Those costs are comparable with estimates from [Cullen (2011)] and [Reguant (2014)]. They are very significant, though much smaller than those for coal generators.

The intercept of fringe generators is estimated to be 2.13. Ignoring shocks to the fringe marginal cost, it sets a lower bound for electricity prices, $8.4/MWh, when there is no fringe generation. When fringe generation increases by 1GW, the marginal costs of fringe generators, and therefore electricity prices, increase by 14.7%.

Table 2: Estimation Results of Cost Parameters

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Gas:Small</th>
<th>Gas: Large</th>
<th>Coal</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\alpha^j$</td>
<td>parameters in the slope of marginal costs ($/MWh)</td>
<td>3.531</td>
<td>0.562</td>
<td>4.727</td>
</tr>
<tr>
<td>$\mu^j$</td>
<td>constant part of marginal costs ($/MWh)</td>
<td>5.427</td>
<td>9.108</td>
<td>5.308</td>
</tr>
<tr>
<td>$\sigma_{\epsilon,j}$</td>
<td>standard deviation of marginal cost unobservables ($/MWh)</td>
<td>1.287</td>
<td>1.132</td>
<td>0.447</td>
</tr>
<tr>
<td>$\kappa_{0,j}$</td>
<td>constant part of startup costs (million $)</td>
<td>0.022</td>
<td>0.000</td>
<td>0.691</td>
</tr>
<tr>
<td>$\kappa_{1,j}$</td>
<td>slope of startup costs (million $)</td>
<td>0.004</td>
<td>0.043</td>
<td></td>
</tr>
<tr>
<td>$\sigma^j$</td>
<td>scale parameters of T1EV shocks (million $)</td>
<td>0.014</td>
<td>0.024</td>
<td>0.078</td>
</tr>
</tbody>
</table>

Panel B. Fringe Generators

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$c_{0,f}$</td>
<td>intercept of fringe marginal costs</td>
<td>2.128</td>
</tr>
<tr>
<td>$c_{1,f}$</td>
<td>slope of fringe marginal costs (per GW)</td>
<td>14.722</td>
</tr>
<tr>
<td>$\sigma^f$</td>
<td>standard deviation of fringe marginal costs</td>
<td>0.1296</td>
</tr>
</tbody>
</table>

Notes: The table reports estimates of generation costs and start-up cost associated with dominant generators and estimates of marginal costs of fringe generators, based on hourly data in ERCOT in 2020. Standard errors are to be added.

Table [A-4] presents profits of different types of generator. Coal generators earn the most annual profits, $19.73 million. Small natural gas generators are the most profitable per MW because natural gas prices were extremely low in 2020.

Finally, I calibrate annual fixed O&M cost as $0.035 million/MW ([Stehly et al. 2020], [Lantz et al. 2016]) for on-shore wind and $0.017 million/MW for distributed solar panels ([Walker et al. 2020], [Wiser et al. 2020]).

5.1.3 Model Fit

To evaluate the model’s performance, I compare data moments with the simulated moments. The exercise shows that, given its parsimonious specification and limited heterogeneity, the model adequately captures the main operational characteristics and approximates aggregate market outcomes. Table 3 compares means and standard deviations of electricity prices and outputs from each type of generator in the data and the average in the model simulations, separately at peak and off-peak hours. They align with each other closely.
Table 3: Electricity Prices and Generation by Type of Generators

<table>
<thead>
<tr>
<th></th>
<th>Off-Peak Hours</th>
<th>Peak Hours</th>
<th>Off-Peak Hours</th>
<th>Peak Hours</th>
</tr>
</thead>
<tbody>
<tr>
<td>Electricity Price ($/MWh)</td>
<td>18.23 (5.29)</td>
<td>20.42 (3.38)</td>
<td>34.22 (20.54)</td>
<td>31.77 (21.69)</td>
</tr>
<tr>
<td>Electricity Generation: Small Gas (GWh)</td>
<td>10.56 (3.24)</td>
<td>11.40 (4.26)</td>
<td>14.26 (2.90)</td>
<td>14.25 (4.76)</td>
</tr>
<tr>
<td>Electricity Generation: Large Gas (GWh)</td>
<td>2.52 (1.35)</td>
<td>2.16 (1.23)</td>
<td>3.46 (1.59)</td>
<td>3.26 (1.87)</td>
</tr>
<tr>
<td>Electricity Generation: Coal (GWh)</td>
<td>7.29 (1.60)</td>
<td>6.92 (2.72)</td>
<td>9.51 (2.32)</td>
<td>9.65 (3.21)</td>
</tr>
</tbody>
</table>

Notes: The table provides a comparison of the means and standard deviations (in parentheses) for electricity prices and outputs between the observed data and the averaged results from model simulations. This comparison is presented separately for both peak hours and off-peak hours.

Table A-5 presents means and standard deviations of utilization factors under different realizations of residual demand. They are calculated when generators operate and neither the minimum output requirement nor capacity is binding. The model reflects the positive correlation between electricity generation and residual demand. It fits particularly well under low and moderate residual demand realizations, which account for the majority of hours.

Table 4 shows that the model also predicts well the start-up decisions of generators. The frequency of turning on after turning off is fitted perfectly between data and model simulations. For coal and large natural gas generators, it also fits well the difference of operational probabilities at peak and off-peak hours. One caveat is that the model underestimates that difference for small gas generators. Table A-6 shows the operational probabilities under different previous operational statuses, by different realizations of residual demand. The model effectively captures the disparities in the operational probabilities under different previous status, especially when realizations of residual demand are low or moderate. However, it tends to overestimate the probability of continuing to operate in two consecutive hours with high residual demand realizations. Table A-7 also presents the probability of switching from off to on, by different realizations of natural gas prices.

Table 4: Start-up Frequency and Probability of Operation

<table>
<thead>
<tr>
<th></th>
<th>Gas: Small</th>
<th>Gas: Large</th>
<th>Coal</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Data</td>
<td>Model</td>
<td>Data</td>
</tr>
<tr>
<td>Pr[start up]</td>
<td>0.10</td>
<td>0.11</td>
<td>0.08</td>
</tr>
<tr>
<td>Pr[on</td>
<td>off-peak hours]</td>
<td>0.63</td>
<td>0.69</td>
</tr>
<tr>
<td>Pr[on</td>
<td>peak hours]</td>
<td>0.80</td>
<td>0.76</td>
</tr>
</tbody>
</table>

Notes: The table presents a comparison between data and model simulations in terms of the probability of start-up — that is, the share of hours when a generator switches from off to on and the probability of operation at off-peak and peak hours. It compares between data and simulations the probability of start up, that is the share of hours when a generator switches from off to on, and the probability of being on during off-peak hours and peak hours.
5.2 Profit Surfaces Linking the Hourly Model with the Annual Model

To compute annual profits within various states \((K_t, z_t)\) for the annual entry and exit model, it is necessary to solve the hourly model \(T\) times in each iteration when solving for the nonstationary oblivious equilibrium. This iterative process may require numerous iterations for the model to reach convergence. Although solving the hourly model individually is efficient, the cumulative time required can become quite substantial.

To accelerate the computation of annual profits while preserving the richness of dynamics in the wholesale electricity market, I solve the hourly model across an extensive range of predetermined values for \((K_t, z_t)\), as indicated in Table A-8. It’s worth noting that the bounds for each variable are chosen generously to ensure that the capacity of each energy source in all counterfactual scenarios falls within the range of evaluation points. This means that when utilizing the approximated profit surface, no extrapolation is involved. Similarly to Bodéré (2023), I then train a deep neural network to approximate the annual profits.\(^{24}\)

To understand the impact of states \((K_t, z_t)\) on profitability of various generator types, Table 5 presents the OLS estimates of the profit surface. The dependent variables are annual profits ($ million/GW) for each generator type, while the independent variables are the states \((K_t, z_t)\). Before discussing the economic findings, it’s noteworthy that the relatively low R-squares observed with natural gas and coal imply significant nonlinearity in the relationship between annual profits and these states. This underscores the critical necessity of employing a deep neural network to approximate the profit surface.

There are three findings from Table 5. First, there are significant competition effects between any two types of energy source. Importantly, the business stealing effects of renewables on coal are almost twice as large as the effects on natural gas. Second, the increase in natural gas prices reduces profits of natural gas generators and increases profits of all the other generators, especially coal generators. Third, the rise in electricity demand provides coal generators with nearly twice the benefit it offers natural gas, while wind and solar gain less from an increase in demand.

\(^{24}\)I use an \(8 \times 32 \times 32 \times 5\) deep neural network in which there are eight input variables \((K_t, z_t)\) and five output variables \((\Pi^j, j \in \{\text{small natural gas, large natural gas, coal, wind, solar}\})\).
### Table 5: Profit Surface ($ million/GW): OLS Approximation

<table>
<thead>
<tr>
<th></th>
<th>Small Natural Gas</th>
<th>Large Natural Gas</th>
<th>Coal</th>
<th>Wind</th>
<th>Solar</th>
</tr>
</thead>
<tbody>
<tr>
<td>$K_{\text{small natural gas}}$ (GW)</td>
<td>-1.937***</td>
<td>-1.781***</td>
<td>-1.830***</td>
<td>-0.575***</td>
<td>-0.325***</td>
</tr>
<tr>
<td></td>
<td>(0.011)</td>
<td>(0.011)</td>
<td>(0.013)</td>
<td>(0.005)</td>
<td>(0.002)</td>
</tr>
<tr>
<td>$K_{\text{large natural gas}}$ (GW)</td>
<td>-2.674***</td>
<td>-2.760***</td>
<td>-2.702***</td>
<td>-0.853***</td>
<td>-0.454***</td>
</tr>
<tr>
<td></td>
<td>(0.044)</td>
<td>(0.044)</td>
<td>(0.056)</td>
<td>(0.019)</td>
<td>(0.010)</td>
</tr>
<tr>
<td>$K_{\text{coal}}$ (GW)</td>
<td>-1.451***</td>
<td>-1.441***</td>
<td>-3.606***</td>
<td>-1.137***</td>
<td>-0.597***</td>
</tr>
<tr>
<td></td>
<td>(0.010)</td>
<td>(0.010)</td>
<td>(0.013)</td>
<td>(0.004)</td>
<td>(0.002)</td>
</tr>
<tr>
<td>$K_{\text{wind}}$ (GW)</td>
<td>-0.720***</td>
<td>-0.704***</td>
<td>-1.622***</td>
<td>-0.828***</td>
<td>-0.366***</td>
</tr>
<tr>
<td></td>
<td>(0.004)</td>
<td>(0.004)</td>
<td>(0.006)</td>
<td>(0.002)</td>
<td>(0.001)</td>
</tr>
<tr>
<td>$K_{\text{solar}}$ (GW)</td>
<td>-0.543***</td>
<td>-0.524***</td>
<td>-1.098***</td>
<td>-0.449***</td>
<td>-0.345***</td>
</tr>
<tr>
<td></td>
<td>(0.004)</td>
<td>(0.004)</td>
<td>(0.005)</td>
<td>(0.002)</td>
<td>(0.001)</td>
</tr>
<tr>
<td>Effects of Energy Storage</td>
<td>-18.874***</td>
<td>-15.525***</td>
<td>-40.248***</td>
<td>-0.913***</td>
<td>-3.239***</td>
</tr>
<tr>
<td></td>
<td>(0.626)</td>
<td>(0.625)</td>
<td>(0.795)</td>
<td>(0.259)</td>
<td>(0.134)</td>
</tr>
<tr>
<td></td>
<td>(0.119)</td>
<td>(0.119)</td>
<td>(0.151)</td>
<td>(0.051)</td>
<td>(0.026)</td>
</tr>
<tr>
<td>Demand Shifter</td>
<td>122.477***</td>
<td>117.552***</td>
<td>243.441***</td>
<td>101.649***</td>
<td>55.710***</td>
</tr>
<tr>
<td></td>
<td>(0.725)</td>
<td>(0.725)</td>
<td>(0.921)</td>
<td>(0.307)</td>
<td>(0.159)</td>
</tr>
<tr>
<td>Constant</td>
<td>114.015***</td>
<td>99.875***</td>
<td>58.948***</td>
<td>31.972***</td>
<td>20.983***</td>
</tr>
<tr>
<td></td>
<td>(1.126)</td>
<td>(1.125)</td>
<td>(1.430)</td>
<td>(0.488)</td>
<td>(0.252)</td>
</tr>
<tr>
<td>Observations</td>
<td>340,558</td>
<td>340,558</td>
<td>340,558</td>
<td>371,520</td>
<td>371,520</td>
</tr>
<tr>
<td>R-squared</td>
<td>0.288</td>
<td>0.265</td>
<td>0.476</td>
<td>0.580</td>
<td>0.601</td>
</tr>
</tbody>
</table>

**Notes:** The table reports OLS estimates of the profit surface. The dependent variable in each column is the profit ($ million/GW) for each type of generator. Independent variables are capacities of each energy source (GW), the effect of energy storage $z^b_t \in [0, 1]$, the electricity demand shifter $z^d_t \in [0.8, 1.6]$ and the natural gas price shifter $z^g_t \in [1, 5]$.

### 5.3 Calibration of Entry Costs and Scrap Values

The parameters to be calibrated in the annual model are summarized in $\Xi_{\text{annual}}$:

$$
\Xi_{\text{annual}} = (\phi_{\text{coal}}, \phi_{\text{natural gas}}, \psi_{\text{coal}}, \psi_{\text{natural gas}}, \{I^\text{wind}_t, I^\text{solar}_t\}_t=0)
$$

The calibration takes two steps. First, I focus on entry costs and mean scrap values associated with coal and natural gas generators. Since no dominant natural gas generator in my sample retired, I calibrate the mean scrap value of natural gas using the discounted present value of annual maintenance costs estimated in Elliott (2022). I calibrate the remaining parameters by aligning trends in capacities of coal and natural gas within the data and model simulations. More precisely, I calibrate the entry

---

25 Since I only observe one realization of entry or exit probability for each type of energy in each year, I cannot estimate the parameters in the annual model in this nonstationary environment.
26 I restrict the entry costs per GW to be same for small and large natural gas generators, and in the following analysis, I sum capacities of small and large generators and report the total as natural gas.
27 Without observing firms’ frequently cycling between operating and not operating, scrap values and fixed costs cannot be separately identified. It is common to assume one of them is zero and estimate the other (Collard-Wexler, 2013). I assume that the mean scrap value is the saving of accumulated annual maintenance (fixed) costs in the future. Therefore, under the infinite-horizon assumption, the mean scrap value is calculated as the maintenance cost divided by $(1 - \beta)$. 

---

28
costs of natural gas generators by matching the capacity increase from 2005 to 2020 in the data with that from model predictions. No dominant coal generator in the sample retired before 2015 and coal entry was essentially forbidden because of environmental regulations after 2015. Therefore, for coal generators, I calibrate entry costs by matching the capacity increase from 2005 to 2015 in data and model predictions, and I calibrate the mean scrap value by matching the capacity reduction between 2015 and 2020 in the same manner.

The calibration proceeds as a nested procedure. In the inner loop, I solve capacities of coal and natural gas across years in the nonstationary oblivious equilibrium, assuming that they have perfect foresight about profit shifters \( \{ z_t \}_{t=0}^T \), and wind and solar capacities, \( \{ K_t^{\text{wind}}, K_t^{\text{solar}} \}_{t=0}^T \). In the outer loop, I search for parameters that best match capacity changes from model predictions with the data. Wind and solar capacities \( \{ K_t^{\text{wind}}, K_t^{\text{solar}} \}_{t=0}^T \) combine both data between 2005 and 2020 and authoritative projections from the [Department of Energy (2023)] and [Asmelash and Prakash (2019)]. Since both historical data and projections are based on the renewable subsidy scheme before 2020, it is appropriate to use them in the calibration procedure; The capacities of wind and solar in the counterfactuals are endogenously determined from the equilibrium in the annual model. Demand and natural gas price shifters are shown in Figure 2. For the effect of energy storage, I assume that \( z_b^T = 0 \) until 2030, as suggested in [Butters et al. (2021)] and they increase linearly until \( z_b^T = 1 \).

Table 6: Parameters Related to Entry and Exit ($ million/GW)

<table>
<thead>
<tr>
<th>Panel A. Entry Costs</th>
<th>Value</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>Natural Gas</td>
<td>923.4</td>
<td>Matching change in natural gas capacity between 2005 and 2020</td>
</tr>
<tr>
<td>Coal</td>
<td>3288.5</td>
<td>Matching change in coal capacity between 2005 and 2015</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Panel B. Mean Scrap values</th>
<th>Value</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>Natural Gas</td>
<td>332.4</td>
<td>[Elliott (2022)]</td>
</tr>
<tr>
<td>Coal</td>
<td>855.8</td>
<td>Matching change in coal capacity between 2015 and 2020</td>
</tr>
</tbody>
</table>

Notes: The table reports the calibration of entry costs and mean scrap values associated with natural gas and coal generators. The calibration procedure is described in Section 5.3.

Table 6 presents the calibration results for coal and natural gas generators. The calibrated value of coal entry cost is $3,288.5 million/GW, which is in the range of engineering estimates ($1800 million/GW in [Schlissel et al. (2008)] to $4,500 million/GW in [ESFC (2023)]. The entry cost of natural gas generators is calibrated to be $923.4 million/GW, about one third that of coal. It is also aligned with engineering estimates between $780 million/GW and $1,110 million/GW according to the Annual Electric Generator Reports of the EIA. The means of scrap values are calibrated as $332 million/GW for natural gas generators and $855 million/GW for coal generators. The scrap values are a combination of saved fixed

---

28The Carbon Pollution Standard for New Plants (Section 111(b)) effectively prohibits the establishment of new coal power plants [Abito et al. (2022)]. Therefore, I assume that \( \psi^{\text{coal}} = \infty \) for coal after 2015.

29I experiment with \( z_b^T \in \{0.2, 0.4, 0.6, 0.8, 1\} \). I find that all of these values give similar calibration values for parameters associated with coal and natural gas. But different trajectories yield different entry costs associated with wind and solar, especially after 2030. Therefore, I choose \( z_b^T = 1 \), which provides the closest calibration of renewable installation costs when compared with engineering estimates.
operational costs in the future and decommissioning costs,\(^{30}\) and my calibration for coal suggests that the former outweighs the latter.

In the second step, I calibrate time-varying installation costs associated with wind and solar. Given the equilibrium coal and natural gas capacity trajectories determined in the first step of calibration, I back out entry costs of wind and solar that are consistent with their historical and projected capacities, using free-entry conditions \(^{(3)}\). Then I add back subsidies renewables received to obtain calibrations of installation costs for wind and solar in each year.

Figure 4b compares the model-calibrated installation costs with the engineering estimates. They align closely with each other. Initially, the installation costs of wind were about half of those of solar. However, installation costs of solar declined rapidly since 2015 and became lower than wind after 2018.

\[\text{Figure 4: Installation Costs: Comparison between Model Calibration and Engineering Estimates}\]

**Notes:** The figures compare installation costs of wind and solar from model calibration with those from engineering estimates.

### 6 Counterfactual Results

In this section, I study the equilibrium effects of renewable subsidies and examine how the lengths of subsidies influence those effects. I solve the entry and exit model described in Section 3 to predict average capacity by energy source under counterfactual subsidies that change the time-varying entry costs of renewables. Then I evaluate the carbon emissions and generation costs by solving the hourly model in each year along the transition path.

\(^{30}\)The decommissioning costs come from utility separation, removal of asbestos and other dangerous materials, managing employees who are no longer able to work at the power plant following its closure, environmental cleanup, and restoring the site to a secure and ecologically sustainable state.

\(^{31}\)I assume that the capacity cap for new entrants is 10GW for each type of generator, about twice the maximum newly built capacity observed in the data. Therefore, the upper bound is never binding in the calibration. I use the engineering estimates for solar before 2018, when there was no solar entry.
6.1 The Effects of Renewable Subsidies

The first counterfactual quantifies the effects of renewable subsidies in place between 2005 and 2020 on carbon emissions, investment, and generation costs by comparing the path with subsidies and the one without them.

Figure 5 plots mean capacities of different energy source with subsidies between 2005 and 2020 with and without subsidies. Without subsidies, there would be no wind and solar until 2030, at which point installation costs would have decreased sufficiently, paving the way for a rapid expansion of renewable capacities. Coal capacity without subsidies increased by 3.8GW, about 22.6% of maximum coal capacity with subsidies. The increase takes place very early in the transition, even though there is only 0.85GW of wind capacity with subsidies. Consequently, the decreased coal expansion under subsidies cannot be explained by a static model. Instead, subsidies that promote more renewables intensify future competition and diminish the appeal of entering the market. Therefore, fewer coal generators can afford their significant entry costs, leading to a reduction of coal expansion. With natural gas generators’ much smaller entry costs, their capacity expands more in the middle of the transition without subsidies, after sufficient retirement of coal generators and before the renewables start to expand.

I assume that after 2020, subsidies phase out linearly until 2030.

The absence of reactions by natural gas generators before 2015 can be attributed to both the expansion of coal and high natural gas prices. Aggressive coal expansion erodes profits of natural gas, and high input prices reduce the benefits that natural gas generators derive from having fewer renewable competitors. Appendix A-3 shows that natural gas capacity will increase without subsidies before 2015 in either of the following two cases. In the first case, I reduce the natural gas price to $4.08/MMBtu whenever it exceeds that limit before 2015. In the second case, the coal expansion is mitigated by a reduction in the capacity cap for new coal generators from 10GW to 5GW.
Figure 5: Transition Paths with and without Subsidy

Notes: The solid blue lines represent mean capacities of different energy sources with subsidies in place between 2005 and 2020. The dashed red lines are capacity paths of different energy sources when subsidies are removed.

Carbon emissions are affected because of changes in the transition path caused by generator entry and exit and changes along the path caused by adjusting their production decisions. Figure 6 displays annual and cumulative carbon emissions since 2005 for the path on which subsidies were present between 2005 and 2020 and that without subsidies. Figure 6b shows that renewable subsidies reduce cumulative carbon emissions by 1.71 billion tons through 2060. They reduce environmental costs by $62-$316 billion, evaluated at the social cost of carbon of $36.6/ton (Carleton et al., 2022) or $185/ton (Rennert et al., 2022). Figure 6a indicates that the increase in carbon emissions from initial coal expansion persists for multiple decades. I further calculate the differences in carbon emissions from coal generation with and without subsidies. I find that 66% of carbon savings can be explained by the deterred coal expansion.
Notes: Panel (a) presents carbon emissions in each year and Panel (b) presents cumulative carbon emissions since 2005. The solid blue lines represent outcomes along the transition path with renewable subsidies in place between 2005 and 2020. The dashed red lines represent counterfactuals in which those renewable subsidies were removed.

In addition to considering environmental effects, I consider the effects of subsidies on economic surpluses, including investment and generation costs. Climate policies are often at the heart of political debate partly because the evaluation of environmental benefits is based on the politically contentious social cost of carbon. Therefore, it is also useful to consider the effectiveness of renewable subsidies solely from an economic standpoint. Figure 7 presents cumulative investment and generation costs over the entire simulation horizon. The investment includes installation costs paid by all new entrants net of the scrap values of retired generators. Through 2060, renewable subsidies save generation costs by $40.9 billion associated with an increase in investment by $14.6 billion. Subsidies increase investment because the earlier adoption of renewables does not reap the benefits from reduction in installation costs in the future. The generation cost reductions mainly come from less natural gas capacity when there are subsidies. That there is more savings of generation costs than extra investment spending implies that renewable subsidies pass the cost-benefit test, even without considering the environmental benefits.
6.2 The Effects of Different Subsidy Horizons

As an important aspect of policy design, the duration of renewable subsidies plays a significant role in determining the timing of renewable expansions and, therefore, in shaping expectations regarding future competition with coal and natural gas. In this section, I study how different lengths of subsidies affect the energy transition. I simulate the transition paths under alternative subsidy horizons and evaluate the surpluses along those counterfactual transition paths. I keep the intensity of subsidies (27$/MWh for PTCs and 30% of installation costs for ITCs) fixed in all simulations. To illustrate the mechanisms, I display the details of transitional dynamics and their impacts for a short-horizon policy between 2005 and 2010 and a long-horizon policy between 2005 and 2032. The results under the scenario with subsidies in place between 2005 and 2020, as a medium-horizon policy, are also presented for comparison purposes. I summarize the effects of subsidies with other horizons in Table 7.

Figure 8 presents the expected capacities of different energy sources. It illustrates how subsidies with a short or long horizon shape the dynamics of energy transition. Panel 8c shows the expected wind capacities, which are the most heavily affected by the subsidies. It demonstrates that the length of subsidies affects the trajectory of wind capacity in two ways. First, the entry of wind power will bunch in years when the subsidies are close to expiring. Under 5-year subsidies, there will be much more wind capacity between 2005 and 2010 compared with longer-horizon subsidies, and after 2010, there will be no wind expansion for the next two decades. Under 27-year subsidies, most wind capacity enters between 2024 and 2032, with no wind entry in either the early phase of transition before 2024 or after 2032. Second, shorter-horizon subsidies only change the timing of renewable entry, with almost no effect on renewable capacity close to the end of transition. However, longer subsidies will change both the timing and the ultimate wind and solar capacities. With installation costs steadily decreasing, the
uniform nature of the PTC received by wind energy is more advantageous compared to the percentage-based ITC, which is primarily applicable to solar energy. Therefore, as shown in Panels 8c and 8d, compared with shorter subsidies, by 2060, 27-year subsidies increase wind capacity by 26.6GW but decrease solar capacity by 36.7GW.

Compared with the medium-horizon subsidies where coal expanded significantly in year 2006, subsidies with shorter or longer horizon can both reduce coal expansions and facilitate a coal-to-gas switch, as illustrated in Panels 8a and 8b in Figure 8. With 5-year subsidies, the rapid expansion of 23.5GW in wind capacity greatly intensifies the competition in the near future for both coal and natural gas. It reduces coal expansion by 4.27GW and also slightly reduces natural gas capacity. Because of the bunching effect, the 27-year subsidies create a vacuum of renewables in the early phase of transition between 2005 and 2020; However, the much more aggressive wind entry in the middle of the transition shifts coal and natural gas generators’ expectations about future competition. Because of their differences in substitution patterns and entry costs, coal and natural gas generators respond differently to the change in the future competition. Coal entry is completely deterred in 2006. After 2010 and before the period when wind starts to expand, there is more natural gas capacity. Compared with the 15-year subsidies between 2005 and 2020, the 27-year subsidies reduce coal capacity by 5.21 GW and replace it with 11.9 GW natural gas capacity.
Notes: The figure plots expected capacities of natural gas, coal, wind, and solar between 2005 and 2060 under subsidies with different horizons. The solid blue lines represent the transition path with subsidies in place between 2005 and 2020, as in Figure 5 for ease of comparison. The dash-dotted black lines represent the transition path with subsidies in place between 2005 and 2032. The dashed red lines represent the transition paths under subsidies between 2005 and 2010.

Differences in transitional dynamics induced by alternative subsidy horizons have implications for both environmental consequences and economic surpluses. Figure 9 displays cumulative carbon emissions and generation costs since 2005 associated with the different subsidy horizons under consideration, and it displays several notable findings. First, even though the longest subsidies have the largest carbon reduction effects, the effects are not monotone in the subsidy horizons. The shorter-horizon subsidies reduce carbon emissions more than the medium-horizon subsidies do. The reason is that the earlier renewable bunching deters the expansion of dirty coal. Second, the effects of cumulative carbon emissions are heterogeneous across time. The cumulative carbon emissions by 2060 are lowest under the 27-year subsidies. However, the carbon emissions before 2030 under 27-year subsidies are uniformly...
higher than the path under 5-year subsidies.

Turning to the impacts on generation costs, unlike with carbon emissions, the 27-year subsidies do not result in as substantial effects as the medium-duration subsidies. This is largely due to the early expansion of high-cost natural gas. Similarly to carbon emissions, the effects on generation costs vary over time. Prior to 2030, the longest subsidies result in the highest electricity generation costs, while the costs peak under the shortest subsidies after 2030.

![Graphs showing cumulative carbon emissions and generation costs over time.](image)

**Figure 9: Effects of Alternative Subsidy Horizons on Carbon Emissions and Generation Costs**

**Notes:** Panel (a) presents cumulative carbon emission, and Panel (b) presents cumulative generation costs, both since 2005. The solid blue lines represent the transition path with subsidies in place between 2005 and 2020, as in Figure 5 for ease of comparison. The dash-dotted black lines represent the transition path with subsidies in place between 2005 and 2032. The dashed red lines represent the transition paths under subsidies between 2005 and 2010.

To compare the performances for different policy horizons, Table 7 reports tax expenditures, savings of generation costs, reduction in environmental costs, and the returns to those tax expenditures spent on renewable subsidies. The economic returns are the ratio between generation cost savings and tax expenditures, and the environmental returns are the saving in environmental costs divided by tax expenditures. The social returns are the sum of these two.

Table 7 reveals a trade-off about the effects of subsidy horizons: the longer horizons deliver more carbon reductions but have lower social returns and economic returns. Among subsidies with horizons shorter than 15 years, the reference case, 10-year subsidies reduce carbon emissions the most, with social returns between 4.84 and 18.97, depending on the value of the social cost of carbon used in the calculation. Subsidies longer than 20 years create much more significant environmental effects. For example, the 21-year subsidies cause approximately 50% more carbon reductions compared with 10-year subsidies, but with much lower returns. Supposing the social objective is to have large enough carbon reduction and on top of that, to achieve highest returns, the approximately optimal subsidy horizon is 21 years.\(^{34}\)

\(^{34}\)The choice of objective function is reasonable because the goal of the climate policies is to reduce carbon
Table 7: Economic and Social Returns to Tax Expenditures on Renewable Subsidies

<table>
<thead>
<tr>
<th>Tax Expenditures ($ billion)</th>
<th>Generation Cost Reduction ($ billion)</th>
<th>Costs of Carbon Reduction ($ billion)</th>
<th>Economic Returns</th>
<th>Environmental Returns</th>
<th>Social Returns</th>
</tr>
</thead>
<tbody>
<tr>
<td>15 years</td>
<td>23.7</td>
<td>[62,131.6]</td>
<td>1.72</td>
<td>[2.62,13.34]</td>
<td>[4.34,15.06]</td>
</tr>
<tr>
<td>1 year</td>
<td>7.7</td>
<td>8.8</td>
<td>1.15</td>
<td>[5.49,27.98]</td>
<td>[6.64,29.13]</td>
</tr>
<tr>
<td>5 years</td>
<td>16.6</td>
<td>23.1</td>
<td>1.39</td>
<td>[4.37,22.27]</td>
<td>[5.76,23.66]</td>
</tr>
<tr>
<td>10 years</td>
<td>21.9</td>
<td>30.3</td>
<td>1.39</td>
<td>[3.45,17.58]</td>
<td>[4.84,18.97]</td>
</tr>
<tr>
<td>15 years</td>
<td>28.5</td>
<td>37.3</td>
<td>1.31</td>
<td>[1.8,9.16]</td>
<td>[3.11,10.47]</td>
</tr>
<tr>
<td>16 years</td>
<td>28.2</td>
<td>40.5</td>
<td>1.43</td>
<td>[2.83,14.42]</td>
<td>[4.26,15.86]</td>
</tr>
<tr>
<td>18 years</td>
<td>36.1</td>
<td>42.3</td>
<td>1.17</td>
<td>[1.45,7.39]</td>
<td>[2.62,8.56]</td>
</tr>
<tr>
<td>21 years</td>
<td>58.7</td>
<td>48.3</td>
<td>0.82</td>
<td>[1.87,9.52]</td>
<td>[2.69,10.34]</td>
</tr>
<tr>
<td>24 years</td>
<td>67.4</td>
<td>47.8</td>
<td>0.71</td>
<td>[1.73,8.79]</td>
<td>[2.43,9.5]</td>
</tr>
<tr>
<td>27 years</td>
<td>75.2</td>
<td>42.0</td>
<td>0.56</td>
<td>[1.56,7.97]</td>
<td>[2.12,8.53]</td>
</tr>
</tbody>
</table>

Notes: The table reports the economic returns, environmental returns, and social returns of tax expenditures on renewable subsidies under alternative time horizons. The economic returns are calculated as the ratio between saving of generation costs and tax expenditures. The environmental returns are the ratio between saving of costs of carbon emissions and tax expenditures. The costs of carbon emissions are reported as an interval; I use $36.6 as the lower bound of the social cost of carbon and $185 as the upper bound. The social returns are the sum of the economic and environmental returns.

7 Conclusion

This paper studies the effects of renewable subsidies on carbon emissions, total investment, and generation costs. The subsidies target clean energy sources, but those effects are realized through equilibrium responses of coal and natural gas generators via both changes in production decisions and entry and exit. To simulate how subsidies change the transition path, I built a nonstationary model of generator entry and exit at the annual level. To determine annual profits, I nested the model with a secondary dynamic model of the wholesale electricity market in which all generators compete to produce electricity every hour and coal and natural gas generators face start-up costs. I applied the models to ERCOT, the electricity grid covering the majority of Texas. I estimated the hourly model using detailed hourly data and calibrated the annual model so that it was consistent with observed and projected capacity changes in ERCOT.

I found that renewable subsidies can reduce cumulative carbon emissions by 1.7 billion tons through 2060 and 66% of the effect comes from reduced coal expansion in the initial year of the transition. The deterrence of coal expansion comes before renewables enter at large scale because the lasting presence of renewable subsidies increases future competition and therefore shifts the expectations of coal generators. Besides their environmental impacts, subsidies reduce costs of generating electricity by $46.5 billion with an extra investment of $14.6 billion, which suggests that despite the environmental benefits from the politically contentious social costs of carbon, the renewable subsidies pass the cost-benefit test from the purely economic perspective.

Besides evaluating the effects of subsidies currently in place, to shed light on better policy designs I studied the impacts of different time horizons of the subsidies. The duration of subsidies has three effects on transitional dynamics: renewables’ bunching, deterrence of coal expansion in the early phase of the transition, and natural gas expansions in the middle phase. The effects have different implications for how different subsidies affect carbon emissions and generation costs, both through the end of the transition and across periods. Among subsidies that cause similarly large carbon reductions, the subsidies lasting for 21 years have the highest social returns to tax expenditures.

This analysis provides a framework to evaluate the effects of a long-lasting policy in a large market with dynamic considerations in both long-run decisions and short-run decisions. Even though applied emission. However, the social returns can play a role when different policies generate similar environmental benefits because the same dollars can be spent in other areas that may generate larger environmental benefits.
to Texas, with suitable modifications the framework can be applied to study the effects of renewable subsidies in other regions or to study other nonstationary policies. The analysis also highlights considerations at play when designing subsidy horizons.

There are two important future directions, building upon the framework presented in this paper. First, given the nature of intermittent generation, more renewable capacity can increase the volatility of the electricity grid. Lacking energy storage, the grid requires generators with lower start-up costs to cycle between on and off multiple times in a day. Low-start-up-cost, high-marginal-cost open-cycle natural gas generators, therefore, can complement renewables. It is therefore important to consider the role of such generators in grid stability in the energy-transition process. Second, through more detailed modeling of battery operations in the hourly model and incorporating the investment costs of the batteries, the framework can be extended to study the equilibrium responses of fossil fuel generators to the development of energy storage, which is important to evaluate the environmental benefits from investing in energy-storage technologies.

\[35\]

When studying the effects of renewable subsidies in a broader region, it may be important to consider learning effects—specifically, endogenous reductions in installation costs of renewables as more capacity is built. It is easy to extend the annual model to incorporate such effects as illustrated in Appendix XXX.
References


Ömer Karaduman. Large scale wind power investment’s impact on wholesale electricity markets. 2021.


I Details in Data Preparation for Estimation

The initial dataset comprises data collected at an hourly frequency throughout a given day. Nonetheless, the model is confined to representing only two hours: a single peak hour and an individual off-peak hour. To facilitate the alignment of the data with the model, I've delineated the peak hour as a time window spanning from 1:00 PM to 8:00 PM, while the off-peak hour encompasses the period from 9:00 PM to 12:00 AM of the subsequent day. By calculating averages within these designated time intervals, I condense electricity demand, electricity prices, renewable output, and electricity generation from each generator into the representation of two model hours.

The process of condensing the on and off statuses of generators presents more complexity, mainly due to the potential occurrence of generator start-ups or shutdowns in the middle of a time window. However, the majority of instances reveal consistent generator statuses, making it feasible to mirror these statuses from the original data. In nearly all cases, if a generator does change its status, it does so only once within a single time window. I define a generator’s status by two scenarios.

In scenarios where a generator exhibit an on(off) state in both the preceding and subsequent hours, yet manifest a status transition within the current time window, I infer the generator to be off(on) for the present hour. Otherwise, I compute the proportion of hours in which the generator is on or off within the time window. This proportion guides the determination of a generator’s status: if the share of on-hours exceeds that of off-hours, the generator’s status is considered on; otherwise, it is categorized as off.

II Algorithm to Solve the Annual Entry/Exit Model

I provide the detailed steps to calculate the non-stationary oblivious equilibrium in the annual entry/exit model described in section 3, following closely Benkard et al. (2008).

III Energy Storage and Curtailment from Renewables in the Hourly Model

Instead of modelling the charging and discharging behaviors of energy storage as Butters et al. (2021), I directly model the effects of energy storage follow Karaduman (2020) as stabilizing residual demand for coal and natural gas generators. Specifically, denote $z^b_t \in [0, 1]$ as a measure of the extent that residual demand is stabilized by energy storage and the residual demand with energy storage $z^b_t$ as $d^b_h(z^b_t)$. Without energy storage, the residual demand is $d^0_h(0) = d_h - (q^W_h + q^S_h)$. With full energy storage, I assume there is no variation in residual demand and $d^1_h(1) = E[d_h] - E[q^W_h + q^S_h]$. With $z^b_t \in (0, 1)$, the residual demand $d^1_h(z^b_t)$ is a convex combination of $d^0_h(0)$ and $d^1_h(1)$

$$d^1_h(z^b_t) = (1 - z^b_t) \times d^0_h(0) + z^b_t \times d^1_h(1)$$

When electricity generation from wind and solar exceeds electricity demand in hour $h$, that is $d^b_h(z^b_t) < 0$, I assume that they will be curtailed proportional to their output respectively in that hour.
Specifically,

\[ Q_{\text{curtailment}}^h = -d_h^c(z_b^d) \times I\{d_h^c(z_b^d) < 0\} \]

\[ q_h^W = K_t^W \omega_h^W - Q_{\text{curtailment}}^h \frac{K_t^W \omega_h^W}{K_h^W \omega_h^W + K_h^S \omega_h^S} \]

\[ q_h^S = K_t^S \omega_h^S - Q_{\text{curtailment}}^h \frac{K_t^S \omega_h^S}{K_h^W \omega_h^W + K_h^S \omega_h^S} \]

**IV Optimal Output and Expected Profits of Dominant Generators**

Conditional on being on, given electricity price \( p_h \), the interior solution of a dominant generator's profit maximization problem is given by

\[ q_{ih}^* = \frac{p_h - (p_j^i H_j^i + \mu^i + \sigma^c \eta_{ih})}{\alpha^i + q_j^i} \eta^i + q_j^i \]

Therefore, subject to the production constraint \([q_j^i, \bar{q}_j^i]\\), the optimal output is given by

\[ q_{ih} = \begin{cases} 
q_{ih}^* \quad \eta_{ih} \in (\eta_{ih}, \bar{\eta}_{ih}) \\
q_j^i \quad \eta_{ih} < \eta_{ih} \\
\bar{q}_j^i \quad \eta_{ih} > \bar{\eta}_{ih} 
\end{cases} \]

where

\[ \eta_{ih} = \frac{p_h - p_j^i H_j^i}{\sigma^c i} \]

\[ \bar{\eta}_{ih} = \frac{p_h - p_j^i H_j^i - \alpha^i \bar{q}_j^i}{\sigma^c i} \]

Integrating out idiosyncratic shocks \( \eta_{ih} \), the expected profits given \( p_h \) is given by

\[^{36}\text{I use the fact that if } \eta \sim \mathcal{TN}(0, 1, a, b), \text{ then} \]

\[ E[\eta] = \frac{\phi(a) - \phi(b)}{\Phi(b) - \Phi(a)} \]

and

\[ E[\eta^2] = 1 + \frac{a\phi(a) - b\phi(b)}{\Phi(b) - \Phi(a)} \]
\[ E[\pi_{ih}|p_h] = \frac{(p_h - p_h^j H^j - \mu_j)^2}{2\alpha_j^2} \phi^j + (p_h - p_h^j H^j - \mu_j)q^j(\Phi(\eta_{ih}) - \Phi(\eta_{ih})) \]

\[-\sigma_{c,j}^2 \left( \frac{(p_h - p_h^j H^j - \mu_j)^2}{\alpha_j^2} \phi^j + q^j \right)(\phi(\eta_{ih}) - \phi(\eta_{ih})) \]

\[ + \frac{(\sigma_{c,j}^2)^2}{2\alpha_j^2} \phi^j(\Phi(\eta_{ih}) - \Phi(\eta_{ih})) + \eta_{ih} \phi(\eta_{ih}) - \eta_{ih} \phi(\eta_{ih}) \]

\[ + \left( (p_h - p_h^j H^j - \mu_j)^2 \phi^j - \frac{\alpha_j^2}{2\phi^j} (\phi^j - q^j)^2 \right) \phi(\eta_{ih}) \]

\[ + \sigma_{c,j}^2 \phi(\eta_{ih}) \]

\[ + (p_h - p_h^j H^j - \mu_j)q^j (1 - \Phi(\eta_{ih})) \]

\[ - \sigma_{c,j}^2 q^j \phi(\eta_{ih}) \]

V Algorithm to Solve the Hourly Competitive Model

I provide the detailed steps to calculate the moment-based equilibrium in the hourly competitive model described in section 4 following Irfrach and Weintraub (2017) and Gowrisankaran et al. (2022).
VI Figures

VI.1 ERCOT Operates an Isolated Grid

Figure A-1: ERCOT Territory
VI.2 Calibration of Installation Costs under Alternative $\frac{b}{T}$

Figure A-2: Comparison of Renewable Installation Costs under Alternative Energy Storage Trajectories

Notes: The figure compares calibration of wind and solar installation costs under alternative trajectories of energy storage. I assume that the effects of energy storage remain zero until 2030 and start to increase linearly. For other assumptions and details about the calibration procedure, see Section 5.3.
VI.3 Additional Counterfactuals when Renewable Subsidies were Removed

![Diagram showing natural gas and coal capacities with and without subsidies.](Image)

**Figure A-3: Additional Counterfactuals when Subsidies were Removed**

*Notes:* The figures provide additional counterfactuals when renewable subsidies were removed to examine why natural gas capacity remains the same as with subsidies before 2015 in Figure 5. The blue solid line represents the natural gas and coal capacity without subsidies, same as Figure 5. The red dash lines represent the natural gas and coal capacities without subsidies when natural gas prices are imposed to be below $4.08 before 2015. The black dash-dot lines represent counterfactual capacities without subsidies when the maximum newly built capacity for coal is reduced from 10GW to 5GW so that coal can only enter less aggressively.
### Table A-1: Summary Statistics by Hours (GWh)

<table>
<thead>
<tr>
<th></th>
<th>Off-peak Hours</th>
<th></th>
<th>Peak Hours</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Mean</td>
<td>SD</td>
<td>Mean</td>
<td>SD</td>
</tr>
<tr>
<td>$d_{th}$</td>
<td>37.21</td>
<td>5.38</td>
<td>45.13</td>
<td>10.06</td>
</tr>
<tr>
<td>$\omega_{W}^h$</td>
<td>0.383</td>
<td>0.154</td>
<td>0.306</td>
<td>0.166</td>
</tr>
<tr>
<td>$\omega_{S}^h$</td>
<td>0.105</td>
<td>0.050</td>
<td>0.404</td>
<td>0.180</td>
</tr>
</tbody>
</table>

**Notes:** The calculation relies on the hourly electricity demand and the utilization factors of wind and solar in ERCOT for the year 2020. Peak hours, which include those between 1:00 PM and 8:00 PM, are consolidated as one, while the remaining hours are grouped as off-peak hours. Subsequently, the average demand and utilization factors are computed for both peak and off-peak hours on a daily basis. Finally, summary statistics are derived from these averaged values.

### Table A-2: Estimates of Demand Shock Process (GWh)

<table>
<thead>
<tr>
<th>VARIABLES</th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>AR(1)</td>
<td>Off-peak hours</td>
<td>Peak hours</td>
</tr>
<tr>
<td>$\rho^d$</td>
<td>0.710***</td>
<td>0.463***</td>
<td>1.577***</td>
</tr>
<tr>
<td></td>
<td>(0.026)</td>
<td>(0.014)</td>
<td>(0.053)</td>
</tr>
<tr>
<td>Observations</td>
<td>731</td>
<td>365</td>
<td>366</td>
</tr>
<tr>
<td>Adjusted R-squared</td>
<td>0.504</td>
<td>0.750</td>
<td>0.710</td>
</tr>
<tr>
<td>$\sigma^d$</td>
<td>5.67</td>
<td>2.69</td>
<td>5.41</td>
</tr>
</tbody>
</table>

**Notes:** Table reports the estimates of demand shock process. Demand shock is the deviation of electricity demand to its mean, by two types of hours. Column (1) group all hours and estimate an AR(1) model, illustrating that the electricity demand is a stationary process overall. Column (2) and (3) estimate two AR(1) model separately for peak hours and off-peak hours. $\sigma^d$ is calculated as the standard deviation of AR(1) residuals.
Table A-3: Wind Productivity Process

<table>
<thead>
<tr>
<th>VARIABLES</th>
<th>(1) AR(1)</th>
<th>(2) Off-peak hours</th>
<th>(3) Peak hours</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\rho^w$</td>
<td>0.632***</td>
<td>0.545***</td>
<td>0.732***</td>
</tr>
<tr>
<td></td>
<td>(0.029)</td>
<td>(0.040)</td>
<td>(0.041)</td>
</tr>
<tr>
<td>Observations</td>
<td>731</td>
<td>365</td>
<td>366</td>
</tr>
<tr>
<td>Adjusted R-squared</td>
<td>0.398</td>
<td>0.341</td>
<td>0.461</td>
</tr>
<tr>
<td>$\sigma^w$</td>
<td>0.124</td>
<td>0.122</td>
<td>0.125</td>
</tr>
</tbody>
</table>

Notes: Table reports the estimates of wind utilization factor process. Wind utilization factor is the ratio of wind generation and capacity, by two types of hours. Column (1) group all hours and estimate an AR(1) model, illustrating that the wind utilization factor is a stationary process overall. Column (2) and (3) estimate two AR(1) model separately for peak hours and off-peak hours. $\sigma^w$ is calculated as the standard deviation of AR(1) residuals.

Table A-4: Decomposition of Profits, by Type of Generators ($\text{million}$)

<table>
<thead>
<tr>
<th></th>
<th>Gas: Small</th>
<th>Gas: Large</th>
<th>Coal</th>
</tr>
</thead>
<tbody>
<tr>
<td>Revenue</td>
<td>37.45</td>
<td>45.99</td>
<td>99.71</td>
</tr>
<tr>
<td>Generation Costs</td>
<td>28.90</td>
<td>36.79</td>
<td>79.78</td>
</tr>
<tr>
<td>Static Profits</td>
<td>8.55</td>
<td>9.21</td>
<td>19.93</td>
</tr>
<tr>
<td>Start-up Costs</td>
<td>2.38</td>
<td>4.75</td>
<td>3.90</td>
</tr>
<tr>
<td>Unobservables</td>
<td>4.21</td>
<td>6.07</td>
<td>3.70</td>
</tr>
<tr>
<td>Profits</td>
<td>10.38</td>
<td>10.52</td>
<td>19.73</td>
</tr>
</tbody>
</table>

Notes: The table reports different components of profits by types of generators, evaluated at the estimated parameters. For the details of computation, see section 4.
Table A-5: Utilization Factors, by Residual Demand (GWh)

<table>
<thead>
<tr>
<th></th>
<th>Gas: Small</th>
<th>Gas: Large</th>
<th>Coal</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Data</td>
<td>Model</td>
<td>Data</td>
</tr>
<tr>
<td>Panel. A Mean</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$E[q</td>
<td>d^r_h &lt; 17.3]$</td>
<td>0.80</td>
<td>0.80</td>
</tr>
<tr>
<td>$E[q</td>
<td>17.3 \leq d^r_h &lt; 26.2]$</td>
<td>0.85</td>
<td>0.84</td>
</tr>
<tr>
<td>$E[q</td>
<td>26.2 \leq d^r_h &lt; 35.2]$</td>
<td>0.88</td>
<td>0.87</td>
</tr>
<tr>
<td>$E[q</td>
<td>35.2 \leq d^r_h &lt; 44.1]$</td>
<td>0.90</td>
<td>0.90</td>
</tr>
<tr>
<td>$E[q</td>
<td>d^r_h \geq 44.1]$</td>
<td>0.93</td>
<td>1.00</td>
</tr>
</tbody>
</table>

Panel.B Standard Deviation

<table>
<thead>
<tr>
<th></th>
<th>Gas: Small</th>
<th>Gas: Large</th>
<th>Coal</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Data</td>
<td>Model</td>
<td>Data</td>
</tr>
<tr>
<td>$SD[q</td>
<td>d^r_h &lt; 17.3]$</td>
<td>0.10</td>
<td>0.11</td>
</tr>
<tr>
<td>$SD[q</td>
<td>17.3 \leq d^r_h &lt; 26.2]$</td>
<td>0.10</td>
<td>0.12</td>
</tr>
<tr>
<td>$SD[q</td>
<td>26.2 \leq d^r_h &lt; 35.2]$</td>
<td>0.09</td>
<td>0.11</td>
</tr>
<tr>
<td>$SD[q</td>
<td>35.2 \leq d^r_h &lt; 44.1]$</td>
<td>0.08</td>
<td>0.11</td>
</tr>
<tr>
<td>$SD[q</td>
<td>d^r_h \geq 44.1]$</td>
<td>0.06</td>
<td>0.03</td>
</tr>
</tbody>
</table>

Notes: The table reports means and standard deviations of utilization factors, conditional on different realizations of residual demand (GWh). For both data and simulations, I restrict observations when generators are on, and neither minimum output requirement nor capacity is not binding.

Table A-6: Operation Probabilities, by Residual Demand (GWh)

<table>
<thead>
<tr>
<th></th>
<th>Gas: Small</th>
<th>Gas: Large</th>
<th>Coal</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Data</td>
<td>Model</td>
<td>Data</td>
</tr>
</tbody>
</table>
| Panel. A Conditional on Not Operating in Previous Hour
| $d^r_h < 1.73$   | 0.10       | 0.16       | 0.05          | 0.05           |      |       |
| $d^r_h \geq 1.73, d^r_h < 2.62$ | 0.22       | 0.29       | 0.09          | 0.11           |      |       |
| $d^r_h \geq 2.62, d^r_h < 3.52$ | 0.35       | 0.49       | 0.28          | 0.24           | 0.05 | 0.03  |
| $d^r_h \geq 3.52, d^r_h < 4.41$ | 0.66       | 0.78       | 0.37          | 0.53           |      |       |
| $d^r_h \geq 4.41$ | 0.82       | 0.96       | 0.66          | 0.88           | 0.21 | 0.33  |
| Panel. B Conditional on Operating in Previous Hour
| $d^r_h < 1.73$   | 0.63       | 0.62       | 0.58          | 0.61           |      |       |
| $d^r_h \geq 1.73, d^r_h < 2.62$ | 0.76       | 0.78       | 0.73          | 0.78           |      |       |
| $d^r_h \geq 2.62, d^r_h < 3.52$ | 0.89       | 0.88       | 0.90          | 0.91           | 0.99 | 0.99  |
| $d^r_h \geq 3.52, d^r_h < 4.41$ | 0.95       | 0.96       | 0.97          | 0.98           |      |       |
| $d^r_h \geq 4.41$ | 1.00       | 1.00       | 0.99          | 1.00           | 0.99 | 0.99  |

Notes: The table reports the probability of being on, depending on whether generators are on or off in the previous hour. They are calculated under different realizations of residual demand (GWh). For natural gas generators, the realizations of residual demand are consolidated into five groups and for coal generators, they are grouped into two categories based on whether they are above 44.1 GWh or not.
Table A-7: Probability of Switching from Off to On, by Natural Gas Prices ($/MMBtu)

<table>
<thead>
<tr>
<th></th>
<th>Small Natural Gas</th>
<th>Large Natural Gas</th>
<th>Coal</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Data Model</td>
<td>Data Model</td>
<td>Data Model</td>
</tr>
<tr>
<td>$p_{Gh}^G &lt; 2.4$</td>
<td>0.39</td>
<td>0.38</td>
<td>0.22</td>
</tr>
<tr>
<td>$p_{Gh}^G &gt; 2.4$</td>
<td>0.28</td>
<td>0.35</td>
<td>0.14</td>
</tr>
</tbody>
</table>

Notes: The table reports the probability of switching from off to on, by different realizations of natural gas prices. They are categorized into two groups based on whether natural gas prices are above $2.4/\text{MMBtu}$ or not.

Table A-8: Pre-specified Points of $(K_t, z_t)$ to Solve the Hourly Model

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Grid Points</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of Small Gas Generators</td>
<td>1 30 60 90 120 160 200 240</td>
</tr>
<tr>
<td>Number of Large Gas Generators</td>
<td>1 10 20 30</td>
</tr>
<tr>
<td>Number of Coal Generators</td>
<td>1 10 20 30 40 80</td>
</tr>
<tr>
<td>Wind Capacity (GW)</td>
<td>10 20 40 60 100 150</td>
</tr>
<tr>
<td>Solar Capacity (GW)</td>
<td>1 20 40 60 100 150</td>
</tr>
<tr>
<td>Effects of energy storage</td>
<td>0, 0.3, 0.6, 0.9</td>
</tr>
<tr>
<td>Natural gas price shifter</td>
<td>1 2 5</td>
</tr>
<tr>
<td>Demand shifter</td>
<td>0.8 1 1.2 1.4 1.6</td>
</tr>
</tbody>
</table>

Notes: The table reports grid points of pre-specified $(K_t, z_t)$ that are used to solve the hourly model and collect annual profits. Note that for small natural gas, large natural gas and coal, instead of directly specifying capacities, I specify the number of generators in each type and then convert them to capacities. The collected annual profits are then used as input to train a deep neural networks to obtain a reliable but computationally fast profit function that serves as payoff in the annual entry/exit model.